## OFFICIAL COMMUNICATIONS

## Meetings of the Society

## New York City, April 24, 1943.

Abstracts must have been in the hands of Associate Secretary T. R. Hollcroft, 531 West 116th St., New York, N. Y., by March 26. By invitation of the Program Committee there will be addresses by Professor R. H. Cameron on Absolutely convergent trigonometric sums and Professor Nelson Dunford on Spectral theory.

## Chicago, Illinois, April 23-24, 1943.

Abstracts must have been in the hands of Associate Secretary W. L. Ayres, Purdue University, Lafayette, Ind., by March 26. By invitation of the Program Committee Professor Emil Artin will give an address entitled The axiomatic treatment of number theory and class field theory.

## Stanford University, California, April 24, 1943.

Abstracts must have been in the hands of Associate Secretary A. D. Michal, California Institute of Technology, Pasadena, Calif., by March 27. By invitation of the Program Committee, Professor A. E. Taylor will deliver an address entitled Analysis in complex Banach spaces. There will be a symposium on applied mathematics at which Professor S. P. Timoshenko will speak on Theory of suspension bridges, Dr. E. G. Keller on Some present nonlinear problems of the electrical and aeronautical industries and Dr. Hsue-shen Tsien on The "limiting line" in mixed subsonic and supersonic flows of compressible fluids.

## New Brunswick, New Jersey, September 11-13, 1943.


#### Abstract

Associate Secretary T. R. Hollcroft, 531 West 116 th St., New York, N. Y., not later than August 6. Abstracts received by August 1 will appear in the September issue of this Bulletin. The Colloquium Lectures on Existence theorems in the calculus of variations will be given by Professor E. J. McShane. By invitation of the Program Committee, Professor Antoni Zygmund will give an address.


## New York, City, October 30, 1943.

Abstracts must be in the hands of Associate Secretary T. R. Hollcroft, 531 West 116 th St., New York, N. Y., not later than October 2. Abstracts received by October 1 will appear in the November issue of this Bulletin. By invitation of the Program Committee, Professor W. T. Martin will give an address entitled Mappings by means of systems of analytic functions of several complex variables.

> J. R. Kline, Secretary of the Society.

Articles for insertion in the Bulletin should be typewritten, double spaced, and the author should keep a complete copy. Papers in algebra and theory of numbers should be sent to Saunders MacLane, 474 Widener, Harvard University, Cambridge, Mass.; in analysis to L. M. Graves, University of Chicago, Chicago, Ill.; in other fields to P. A. Smith, Columbia University, New York, N. Y. Reviews should be sent to Virgil Snyder, Brown University, Providence, R. I., and items for Notes to Bulletin of the American Mathematical Society, 531 West 116th St., New York, N. Y. All other communications to the editors should be addressed to the Managing Editor, Tomlinson Fort, Lehigh University, Bethlehem, Pa.

The initial fees and annual dues of members of the Society (see this Bulletin, May, 1930, p. 322; and September, 1942, Part 2, pp. 89-90) are payable to the Treasurer of the Society, B. P. Gill, 531 West 116th St., New York, N. Y.

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