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## ON SELF DUAL L C A GROUPS

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DEFINITION 1.1. Let G be a locally compact Hausdorff Abelian group with a character group  $G^*$ . (Hereafter we shall call such groups G as L C A groups.) G is called self dual if there is a topological isomorphism  $T: G^* \rightarrow G$  from G onto  $G^*$ . Some examples of self dual groups are known in literature, but the structure of all such groups is an open problem (see page 423 of [1]). In this note we announce the structure of those self dual groups which are torsion free as abstract Abelian groups. We state some definitions before announcing the main theorem. The complete details will appear elsewhere.

DEFINITION 1.2. Let J be an index set. Let  $G_{\alpha}$  be an L C A group for each  $\alpha \in J$ . Let  $H_{\alpha} \subset G_{\alpha}$  be a compact, open subgroup of  $G_{\alpha}$  for every  $\alpha \in J$ . By the local direct sum G of the groups  $G_{\alpha}$  modulo  $H_{\alpha}$ , we mean the subgroup of  $\prod_{\alpha \in J} G_{\alpha}$  consisting of those elements for which all but a finite number of coordinates lie in  $H_{\alpha}$ . Notice that  $H = \prod_{\alpha \in J} H_{\alpha}$  is contained in G. We topologise G in such a way that H is declared to be open in G, and the relative topology on H as a subspace of G coincides with the product topology of the spaces  $H_{\alpha}$  where  $H_{\alpha}$  is given the relative topology from  $G_{\alpha}$ . We write  $G = \sum_{\alpha \in J} G_{\alpha}$ . With this definition G is also an L C A group.

DEFINITION 1.3. Let p be a prime integer > 0. Then  $J_p$  denotes the field of p-adic numbers with usual addition and topology. With this addition and topology,  $J_p$  is a locally compact Abelian group. Any compact, open subgroup  $H_p$  of  $J_p$  is called p-adic integers. A local direct sum  $\sum_{\alpha \in X} G_{\alpha}$  of the L C A groups  $G_{\alpha}$  is called a canonical p-group if each  $G_{\alpha}$ , where  $\alpha \in X$ , is isomorphic to p-adic numbers and, in each  $G_{\alpha}$ , some compact open subgroup is fixed in advance.

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THEOREM. Let G be a torsion free Abelian group. Let it further be a locally compact group in some topology. Then G is self dual if and only if G is the direct product  $R^n \times D \times D^* \times H$ , where  $R^n$  is the real n-dimensional Euclidean space  $(n \ge 0)$  and D is a discrete, torsion free divisible group and  $D^*$  is its dual and H is the local direct sum  $\sum_{p \in \mathfrak{J}} G_p$  of canonical p-groups  $G_p$  and  $\mathfrak{J}$  is a collection of primes.

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