

AMERICAN MATHEMATICAL SOCIETY



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Susan Friedlander Chief Editor

Book Reviews

Robert L. Devaney

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