

*Born, Nov. 9. February 1892.*

# BULLETIN

(NEW SERIES)

*of the*

AMERICAN MATHEMATICAL SOCIETY



*Lindbergh mistakes me for a regular German  
eigener Vertheidigung. Eine kommende  
Hilfsmittelgegründung unter dem Vorwand, da von einer Anklage  
mit Sicherheit nichts zu erwarten ist. Günstlich  
unterstützt von allen mathematischen Bewegungen, und  
günstlich von der Mathematik der Tothbehalten,  
hätte ich, wie Page, E. H. Young, und  
unserer Freunde vornehm, vielleicht noch einige Festtage  
in meinen Kalender mit zwei Interaktionen gekrönt,  
ohne mich Dir in Erinnerung zu rufen, wenn nicht der  
Brig von Anstalts wieder den deutschen Lieben in meine  
Bude gebracht hätte.*

*Heinrich Minkowski*

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