



BULLETIN

(NEW SERIES)

of the

AMERICAN MATHEMATICAL SOCIETY

THE ELEMENTS

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of the most aunci-
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Whereunto **Editors** *certaine
Scholies, Annotations, and Inven-
tions, of the best Mathematici-
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in this our*

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Book Reviews

Robert L. Devaney

*With a very fruitfull Preface made by M. I. Dee,
specifying the chiefe Mathematicall Sciēces, what
they are, and wherunto commodious: where, also, are
disclosed certaine new Secrets Mathematicall
and Mechanicall, untill these our daies, greatly missed.*

VOLUME 49

NUMBER 1

JANUARY 2012

Arithmetica

Available electronically at
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Bulletin (New Series) of the American Mathematical Society

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Bulletin (New Series) of the American Mathematical Society (0273-0979) is published quarterly by the American Mathematical Society at 201 Charles Street, Providence, RI 02904-2294 USA. Periodicals postage is paid at Providence, Rhode Island, and additional mailing offices. POSTMASTER: Send address changes to *Bulletin*, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA.

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This journal is indexed in *Mathematical Reviews*, *Science Citation Index*[®], *Science Citation Index*TM-Expanded, *ISI Alerting Services*SM, *CompuMath Citation Index*[®], and *Current Contents*[®]/*Physical, Chemical & Earth Sciences*. This journal is archived in *Portico*.
Printed in the United States of America.

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10 9 8 7 6 5 4 3 2 1 17 16 15 14 13 12

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American Mathematical Society Distribution Center
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Bulletin (New Series) of the Amer. Math. Soc.

VOLUME 49

NUMBER 1

PAGES 1–186

JANUARY 2012



0273-0979(201201)49:1;1-T