

SYMPOSIUM ON

Algebraic Topology in Honor of José Adem

AMERICAN MATHEMATICAL SOCIETY



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CONTEMPORARY MATHEMATICS Volume 12

SYMPOSIUM ON Algebraic Topology in Honor of José Adem

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Introduction

On August 10, 1981 and for one week, we had a conference on Algebraic Topology in Oaxtepec, Morelos, Mexico. The occasion for this conference was to celebrate José Adem's 60th birthday. We were very proud to see it happen with so many of his friends, students and admirers.

I have had the pleasure to be in close contact with José over the past twenty years, both as a friend, colleague and collaborator.

He has lived all this time with one goal: To create the proper atmosphere in Mexico so that we scientists can do research subject only to two conditions: quality and continuity.

With his own life as an example, he has been a guide to many generations of young mathematicians and scientists.

The meeting was possible due to the generous financial assistance of the Centro de Ivestigacion del IPN, Consejo Nacional de Ciencia y Tecnologia, Instituto Politecnico Nacional, Subecretaria de Educacion Superior e Ivestigacion Tecnologica and Subecretaria de Educarion Superior e Investigacion.

I want to thank all the participants and contributors for their warm cooperation, and offer José this volume to commemorate the event and as a token of our commitment to his goal.

> Samuel Gitler Jerusalem June 1982

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LIST OF PARTICIPANTS

ADAMS, Frank Department of Pure Mathematics and Mathematical Statistics University of Cambridge 16 Mill Lane, Cambridge CB2 1SB England ADEM, Alejandro UNAM Estudiante ADEM. José Dirección CINVESTAV Apdo, Postal 14-740 México 14, D.F. AGUILAR, Gerardo UNAM Estudiante AGUILAR, Marcelo Mathematics Institute University of Warwick Coventry, CV4 7AI England ANTONIANO, Enrique Depto. de Matemáticas CINVESTAV Apdo. Postal 14-740 Mexico 14, D.F. ASTEY, Luis Depto. de Matemáticas CINVESTAV Apdo. Postal 14-740 Mexico 14, D.F.

BOYER, Charles Harvard University Mathematics Department Cambridge, MA 02138 USA

BRACHO, Javier 60 Wadsworth Street 10A Cambridge, MA 02142 USA

BROWDER, William Princeton University Department of Mathematics Fine Hall - Box 37 Princeton, NJ 08544 USA

BROWN, Edgar H. Jr. Department of Mathematics Brandeis University Waltham, MA 02154 USA

CLAPP, Mónica Instituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F.

COHEN, Fred Department of Mathematics University of Kentucky Lexington, KY 40506

DAVIS, Donald Department of Mathematics Leigh University Bethlehem, PA 18015 USA

LIST OF PARTICIPANTS

DOLD, Albrecht Mathematisches Insitut Universitaet Heidelberg 6900 Heidelberg 1, Den West Germany GARCIA-MAYNEZ, Adalberto Instiuto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. GITLER, Samuel Mathematics Department Brandeis University Waltham, MA 02154 USA GOMEZ-MONT, Xavier Insituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. GONZALEZ ACUÑA, Francisco Instituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. GUTIERREZ, Angela GUTIERREZ, Mauricio Mathematics Department Tufts University Medford, MA 02155 USA HAEFLIGER, André Institute for Advanced Studies Department of Mathematics Princeton, NJ 08540 USA

HERNANDEZ, Luis Instituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. HUNT, John Departamento de Matemáticas CINVESTAV Apdo. Postal 14-740 México 14, D.F. JIMENEZ REYES, Jesús LAM, Kee Y. The University of British Columbia 2075 Wesbroock Mall Vancouver, B.C. Canada V6T IW5 LIULEVICIUS. Arunas Department of Mathematics The University of Chicago 5734 Univ. Avenue Chicago, IL 60637 USA LLUIS, Emilio Instituo de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. MASSEY, William Department of Mathematics Yale University Box 2155 Yale Station New Haven, CT 06520 USA

MAHOWALD, Mark Department of Mathematics College of Arts & Sciences Northwestern University Evanston, IL 60201 USA MAY, Peter The University of Chicago Department of Mathematics 5734 Univ. Avenue Chicago, IL 60637 USA MEJIA, Janitzio Department de Matemáticas CINVESTAV Apdo, Postal 14-740 México 14. D.F. MILGRAM, James Department of Mathematics Stanford University Stanford, CA 94305 USA MONTEJANO, Luis Instituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. MOORE, John Princeton University Department of Mathematics Fine Hall - Box 37 Princeton, NJ 08544 USA MORAVA, Jack John Hopkins University Department of Mathematics Baltimore, MD 21218 USA

NEYMET, Silvia de Instituto de Mathemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. PAEZ, Javier PETERSON, Franklin Massachusetts Institute of Technology Mathematics Department Cambridge, MA 02139 USA PRIETO, Carlos Instituto de Matemáticas Area Científica Circuito Exterior Cd. Universitaria México 20, D.F. RANDALL, Duane Pontificia Universidade Católica Rua Marques de São Vicente 209/263 Río de Janeiro 22453, RJ Brasil RAVENEL, Douglas Department of Mathematics University of Washington Seattle, WA 98195 USA REES, Elmer Department of Mathematics University of Edinburgh James Clerk Maxwell Building The King's Building, May Fild Road Edinburgh, EH9 3JZ England

LIST OF PARTICIPANTS

SCHWEITZER, Paul Institute for Advanced Studies Department of Mathematics Princeton, NJ 08540 USA SEADE. José Instituto de Matemáticas Area Cientifica Circuito Exterior Cd. Universitaria México 20. D.F. SIRVENT, Martiza Facultad de Ciencias Depto, de Matemáticas Cd. Universitaria México 20, D.F. SNAITH, Victor Faculty of Science Department of Mathematics The University of Western Ontario London, Canada N6A 5B9 SOBERON, Socorro Instituto de Matemáticas Area Cientifica Circuito Exterior Cd. Universitaria México 20, D.F. SPANIER, Edwin University of California Berkeley Department of Mathematics Berkeley, CA 94720 USA SUNDARARAMAN, Dariswami CINVESTAV Depto. de Matemáticas Apdo. Postal 14-740 México 14. D.F.

VALDIVIA, Oscar Panamá 9-1- Panamá Apdo. Postal 109 PANAMA

VALLEJO, Ernesto

VERJOVSKY, Alberto CINVESTAV Depto. de Matemáticas Apdo. Postal 14-740 México 14, D.F.

WILSON, Stephen John Hopkins University Department of Mathematics Baltimore, MD 21218 USA

ZABRODSKY, Alexander The Hebrew University of Jerusalem Department of Mathematics Jerusalem, Israel

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