CONTEMPORARY MATHEMATICS

Graphs and Algorithms

Proceedings of a Summer Research Conference held June 28-July 4, 1987

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Graphs and Algorithms

GOMEMPORARY MATHEMATICS

Volume 89

Graphs and Algorithms

Proceedings of the AMS-IMS-SIAM
Joint Summer Research Conference
held June 28—July 4, 1987 with support
from the National Science Foundation

R. Bruce Richter, Editor

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CONTENTS

Foreword	XI
Organizing Committee	xiii
List of Participants	xiii
The Robertson-Seymour theorems: A survey of applications MICHAEL R. FELLOWS	1
On genus-reducing and planarizing algorithms for embedded graphs JOAN P. HUTCHINSON	19
Interval hypergraphs ARNOLD L. ROSENBERG	27
Competitive algorithms for on-line problems MARK S. MANASSE, LYLE A. McGEOCH, and DANIEL D. SLEATOR	45
On recognizability of planar graphs LARRY I. BASENSPILER	55
Combinatorial computation of moduli dimension of Nielsen classes of covers MIKE FRIED	61
Labeled trees and the algebra of differential operators ROBERT GROSSMAN and RICHARD G. LARSON	81
Computing edge-toughness and fractional arboricity ARTHUR M. HOBBS	89
Directed graphs and the compaction of IC designs BRADLEY W. JACKSON	107
Parallelism, preprocessing, and reachability PHILIP N. KLEIN	129
A summary of results on pair-connected reliability PETER J. SLATER	145

x CONTENTS

On minimum cuts of cycles and maximum disjoint cycles JAYME L. SZWARCFITER	153
Graphs and finitely presented groups ANDREW VINCE	167
Problem corner	187

FOREWORD

The GRAPHS AND ALGORITHMS week of the Joint Summer Research Conference in the Mathematical Sciences took place in Boulder, Colorado, June 28 to July 4, 1987. The co-chairs were Joe Buhler and Phyllis Chinn.

The purpose of the week was to foster communication between computer scientists and mathematicians. Recent work in graph theory and related algorithms has relied on increasingly sophisticated mathematics. Wagner's Conjecture, self-adjusting data structures, graph isomorphism and various embedding and labelling problems in VLSI are examples. Thus, it is clear that researchers in both computer science and mathematics need to be aware of what the other is doing.

The organizers were pleasantly surprised at the depth and diversity of the work being done. The wide range of talks demonstrated the vitality of the activity in both fields. The common graph-theoretic and algorithmic themes insured sufficient cross-interest so many people profited from discussions with others whose work had led in different directions. We hope the papers included here capture some of the diversity and excitement of the conference.

The organizing committee would like to thank all those who attended for their participation. We would also like to thank the AMS-IMS-SIAM Committee and the National Science Foundation for their support. We especially appreciate the hard work of Carole Kohanski of the AMS. The University of Colorado at Boulder was an excellent host institution.

The Organizing Committee



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