

CONTEMPORARY MATHEMATICS

Commutative Harmonic Analysis

Proceedings of a SLU-GTE Conference
held July 27–29, 1987

AMERICAN MATHEMATICAL SOCIETY

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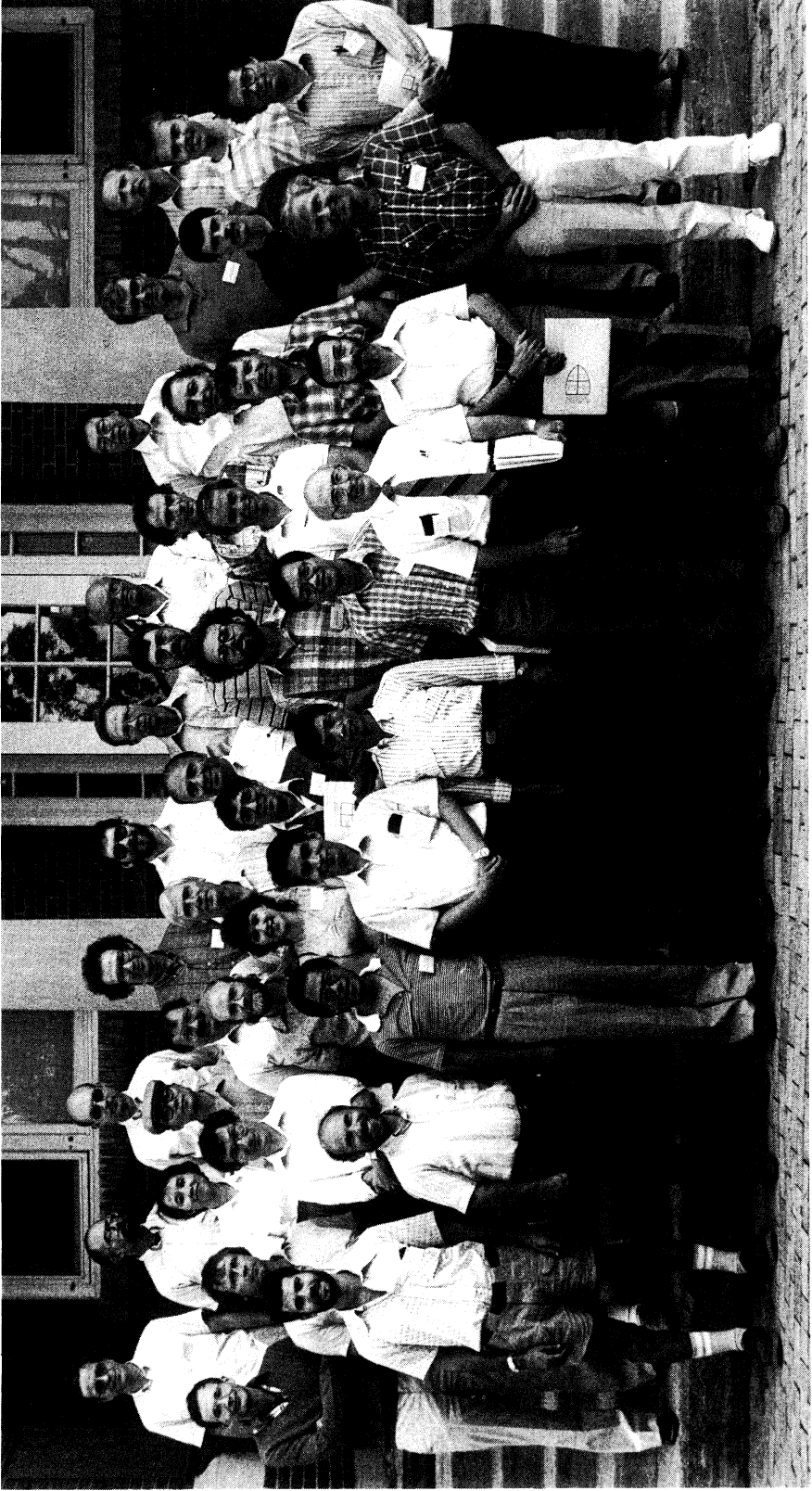
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Commutative Harmonic Analysis



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Volume 91

Commutative Harmonic Analysis

**Proceedings of a SLU-GTE Conference
held July 27–29, 1987**

**with support from St. Lawrence University and
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David Colella, Editor

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INTRODUCTION

This volume represents the proceedings of the SLU–GTE Summer Conference on Commutative Harmonic Analysis held at St. Lawrence University on July 27–29, 1987. It should be noted that some of the papers in this proceedings were not presented at the conference, and not all of the contributing speakers submitted manuscripts.

I would like to thank the General Telephone and Electronics Corporation (GTE) FOCUS program and St. Lawrence University (SLU) for providing the funds making this conference possible. My warmest thanks go to each of the Principal Speakers: Yngve Domar, Uppsala University, Sweden; S. W. Drury, McGill University, Canada; Colin C. Graham, Northwestern University, USA; T. W. Körner, Cambridge University, England; O. Carruth McGehee, Louisiana State University, USA; Jean–François Méla, University of Paris, France; Sadahiro Saeki, Kansas State University, USA. I also thank the conference participants, and the many who supplied me with organizational assistance or advice. Finally, I thank Faye Weeks for the difficult task of typing the manuscripts for this volume.

