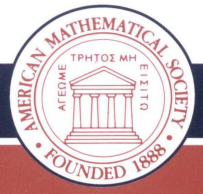

CONTEMPORARY MATHEMATICS

AMERICAN MATHEMATICAL SOCIETY

107

Harmonic Analysis and Partial Differential Equations

Proceedings of a Conference
held April 4–5, 1988

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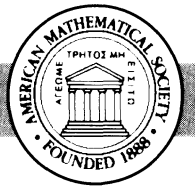
Harmonic Analysis and Partial Differential Equations



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Harmonic Analysis and Partial Differential Equations

Proceedings of a Conference
held April 4–5, 1988

Mario Milman and Tomas Schonbek,
Editors

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Preface

In this volume we have collected, in final form, papers presented at the conference on Harmonic Analysis and Partial Differential Equations held April 4–5, 1988 at Florida Atlantic University.

We thank the participants for their contributions which reflect the quality and the substance of the conference. We are also grateful to Florida Atlantic University for the financial support that made the program possible. A number of people contributed their time and energy helping to make the conference a success, in particular we thank Beth Broer, Jack Freeman, and Vanda Milman.

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