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## 120 Selfadjoint and nonselfadjoint operator algebras and operator theory, Robert S. Doran, Editor

## Selfadjoint and Nonselfadjoint Operator Algebras and Operator Theory

# CONTEMPORARY Mathematics 

# Selfadjoint and Nonselfadjoint Operator Algebras and Operator Theory 

Proceedings of the CBMS Regional Conference held May 19-26, 1990
at Texas Christian University, Fort Worth, Texas with support from the National Science Foundation

Robert S. Doran<br>Editor



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To Shirley and Dave

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## Preface

In May, 1990, a week long conference on operator algebras was held at Texas Christian University in Fort Worth, Texas. The conference was one of the series organized under the auspices of the Conference Board of the Mathematical Sciences (CBMS) and the National Science Foundation. Professor Paul S. Muhly of the University of Iowa gave ten lectures during the week under the title Coordinates in Operator Algebra: Groupoids and Categories, their Representations and Applications. A volume containing Professor Muhly's lectures will be published separately from the present one by the American Mathematical Society in the CBMS-Regional Conference Series.

During the week twenty-eight talks, in addition to Dr. Muhly's, were given by participants. These talks covered a broad spectrum (no pun intended) of topics of current interest in operator algebra and operator theory. This volume contains slightly expanded versions of most of these. The editor, who also served as Conference Director, encouraged those planning to attend to bring some of their favorite open problems. Many did and as a result there are more than one hundred problems and questions scattered throughout this volume. It is hoped that these will serve to stimulate further research in the various areas considered.

Those papers that are in final form and will not appear elsewhere are clearly indicated in a footnote at the bottom of the first page of the article.

The editor wishes to express his sincere gratitude and thanks to all who made possible this volume and the CBMS-Conference. Special thanks go to the NSF for their financial support and to Paul Muhly for agreeing to prepare and give ten lectures (even when loaded down with administrative duties) and then for his masterful job of delivering them. All of us at the conference salute him for a virtuoso performance! Special thanks also to Texas Christian University for hosting yet another conference on mathematics, to my wife Shirley Doran for a beautiful job of preparing the manuscripts in $\mathcal{A} \mathcal{M} \mathcal{S}-\mathrm{T}_{\mathrm{E}} \mathrm{A}$, and to my colleague David Addis for his invaluable help with our computers in the production of this volume.

I wish to thank all of the participants who attended the conference, especially those who presented papers and contributed to this volume. Finally, it is a pleasure to acknowledge the help and support of the American Mathematical Society in the preparation and publication of these proceedings.

Robert S. Doran

Conference Participants



1. Lida Shadabi, 2. Ed Bednarek, 3. Guoliang Yu, 4. Zhong-jin Ruan, 5. Yiu Tung Poon, 6. Ximena Catepillan, 7. Kichi-Suke Saito, 8. Shirley Doran, 9. Paul Muhly, 10. Bob Doran, 11. Keren Yan, 12. Dick Kadison, 13. Shuang Zhang, 14. N. Sivaramakrishnan, 15. Elias Katsoulis, 16. Chaoxin Qiu, 17. Baruch Solel, 18. Xingde Dai, 19. Jim Wright, 20. Bill Paschke, 21. Héctor Salas, 22. Norberto Salinas, 23. Efton Park, 24. Steve Wright, 25. Arlan Ramsay, 26. Frank Gilfeather, 27. Fred Shultz, 28. Takehiko Yamanouchi, 29. Palle E. T. Jorgensen, 30. Aristides Katavolos,
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