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American Mathematical Society

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127

Geometry and Nonlinear Partial Differential Equations

Proceedings of the AMS Special Session
held March 23–24, 1990

Vladimir Oliker
Andrejs Treibergs
Editors



American Mathematical Society
Providence, Rhode Island

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Preface

In March of 1990, at the AMS meeting in Fayetteville, Arkansas, a Special Session on recent developments in “Geometry, Physics, and Nonlinear PDE’s” was held. For this conference, we invited specialists working in the areas of Monge-Ampere equations, prescribed curvature problems, mean curvature, harmonic maps, evolution with curvature dependent speed, isospectral manifolds, and general relativity. In recent years, there has been an enormous surge of activity in the above areas and we received an overwhelming response to our invitations. Twenty-five thirty-minute addresses were delivered in the Session. The majority of papers in the present volume are expositions of these addresses.

We thank all our colleagues who participated in the Session and contributed to this volume. We are indebted to the American Mathematical Society for the generous help with the organization of the Session and publishing of its Proceedings.

Vladimir Oliker
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