# **CONTEMPORARY MATHEMATICS**

## 218

# Domain Decomposition Methods 10

The Tenth International Conference on Domain Decomposition Methods August 10–14, 1997 Boulder, CO

> Jan Mandel Charbel Farhat Xiao-Chuan Cai Editors



American Mathematical Society

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218

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The Tenth International Conference on Domain Decomposition Methods August 10–14, 1997 Boulder, CO

> Jan Mandel Charbel Farhat Xiao-Chuan Cai Editors



American Mathematical Society Providence, Rhode Island

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This volume contains the proceedings of the Tenth International Conference on Domain Decomposition Methods for Partial Differential Equations, which took place at the University of Colorado at Boulder, August 10–August 14, 1997. The focus of the conference was on realistic applications in structural mechanics, structual dynamics, computational fluid dynamics, and heat transfer. The volume is divided into four parts: the first part contains invited papers; the rest of the volume contains minisymposia and contributed presentations, further divided into Algorithms, Theory, and Applications.

Support was provided by the National Science Foundation, ANSYS, Inc., the Sandia National Laboratories, the Colorado School of Mines, the University of Colorado at Boulder, and the University of Colorado at Denver.

> 1991 Mathematics Subject Classification. Primary 65–06; Secondary 65N55, 65M55, 65Y05, 73–06, 76–06.

#### Library of Congress Cataloging-in-Publication Data

International Conference on Domain Decomposition Methods for Partial Differential Equations (1997 : Boulder, Colo.)

Domain decomposition methods 10 : the Tenth International Conference on Domain Decomposition Methods, August 10–14, 1997, Boulder, Colorado, USA / Jan Mandel, Charbel Farhat, Xiao-Chuan Cai, editors.

p. cm. — (Contemporary mathematics, ISSN 0271-4132; 218)

Includes bibliographical references.

ISBN 0-8218-0988-1 (pbk. : alk. paper)

1. Decomposition method—Congresses. 2. Differential equations, Partial—Congresses. I. Mandel, Jan. II. Farhat, Charbel. III. Cai, Xiao-Chuan, 1962–. IV. Title. V. Series: Contemporary mathematics (American Mathematical Society); v. 218. QA402.2.I57 1997

515'.353—dc21

98-15580 CIP

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## Contents

Preface	xi
Part 1. Invited Presentations	1
Nonmatching Grids for Fluids Yves Achdou, Gassan Abdoulaev, Jean-Claude Hontand, Yuri A. Kuznetsov, Olivier Pironneau, and Christophe Prud'homme	3
A Parallel Non-Overlapping Domain-Decomposition Algorithm for Compressible Fluid Flow Problems on Triangulated Domains TIMOTHY J. BARTH, TONY F. CHAN, AND WEI-PAI TANG	23
A Non-Overlapping Domain Decomposition Method for the Exterior Helmholtz Problem ARMEL DE LA BOURDONNAYE, CHARBEL FARHAT, ANTONINI MACEDO, FRÉDÉRIC MAGOULÈS, AND FRANÇOIS-XAVIER ROUX	2 , 42
An Agglomeration Multigrid Method for Unstructured Grids TONY F. CHAN, JINCHAO XU, AND LUDMIL ZIKATANOV	67
Solution of Coercive and Semicoercive Contact Problems by FETI Domain Decomposition ZDENĚK DOSTÁL, ANA FRIEDLANDER, AND SANDRA A. SANTOS	82
An Iterative Substructuring Method for Elliptic Mortar Finite Element Problems with Discontinuous Coefficients MAKSYMILIAN DRYJA	94
Domain Decomposition Methods for Flow in Heterogeneous Porous Media MAGNE S. ESPEDAL, KARL J. HERSVIK, AND BRIT G. ERSLAND	104
A Fictitious Domain Method with Distributed Lagrange Multipliers for the Numerical Simulation of Particulate Flow ROLAND GLOWINSKI, TSORNG-WHAY PAN, TODD I. HESLA, DANIEL D. JOSEPH, AND JACQUES PERIAUX	121
Domain Decomposition Algorithms for Saddle Point Problems LUCA F. PAVARINO	138
Parallel Implementation of Direct Solution Strategies for the Coarse Grid Solvers in 2-level FETI Method FRANÇOIS-XAVIER ROUX AND CHARBEL FARHAT	158
Domain Decomposition and Multi-Level Type Techniques for General Sparse Linear Systems YOUSEF SAAD, MARIA SOSONKINA, AND JUN ZHANG	174

Spectral/ $hp$ Methods for Elliptic Problems on Hybrid Grids Spencer J. Sherwin, Timothy C.E. Warburton, and George Em Karniadakis	191
Physical and Computational Domain Decompositions for Modeling Subsurface Flows	;
Mary F. Wheeler and Ivan Yotov	217
Part 2. Algorithms	229
Nonoverlapping Domain Decomposition Algorithms for the <i>p</i> -version Finite Element Method for Elliptic Problems ION BICĂ	231
A 2-level and Mixed Domain Decomposition Approach for Structural Analysis DAVID DUREISSEIX AND PIERRE LADEVÈZE	238
Iso-P2 P1/P1/P1 Domain-Decomposition/Finite-Element Method for the Navier-Stokes Equations SHOICHI FUJIMA	246
Overlapping Nonmatching Grids Method: Some Preliminary Studies SERGE GOOSSENS, XIAO-CHUAN CAI, AND DIRK ROOSE	254
Nonconforming Grids for the Simulation of Fluid-Structure Interaction Céline Grandmont and Yvon Maday	262
Hash-Storage Techniques for Adaptive Multilevel Solvers and Their Domain Decomposition Parallelization MICHAEL GRIEBEL AND GERHARD ZUMBUSCH	271
Extension of a Coarse Grid Preconditioner to Non-symmetric Problems CAROLINE JAPHET, FRÉDÉRIC NATAF, AND FRANÇOIS-XAVIER ROUX	279
On the Interaction of Architecture and Algorithm in the Domain-based Parallelization of an Unstructured-grid Incompressible Flow Code DINESH K. KAUSHIK, DAVID E. KEYES, AND BARRY F. SMITH	287
Additive Domain Decomposition Algorithms for a Class of Mixed Finite Element Methods AXEL KLAWONN	296
Non-conforming Domain Decomposition Method for Plate and Shell Problems CATHERINE LACOUR	304
Solutions of Boundary Element Equations by a Flexible Elimination Process CHOI-HONG LAI AND KE CHEN	311
An Efficient FETI Implementation on Distributed Shared Memory Machines with Independent Numbers of Subdomains and Processors MICHEL LESOINNE AND KENDALL PIERSON	318
Additive Schwarz Methods with Nonreflecting Boundary Conditions for the Parallel Computation of Helmholtz Problems LOIS C. MCINNES, ROMEO F. SUSAN-RESIGA, DAVID E. KEYES, AND HAFIZ M. ATASSI	325

|--|

On the Reuse of Ritz Vectors for the Solution to Nonlinear Elasticity Problems by Domain Decomposition Methods	3
Dual Schur Complement Method for Semi-Definite Problems	941
DANIEL J. KIXEN	341
Two-level Algebraic Multigrid for the Helmholtz Problem PETR VANĚK, JAN MANDEL, AND MARIAN BREZINA	349
A Comparison of Scalability of Different Parallel Iterative Methods for Shallow Water Equations ARNT H. VEENSTRA, HAI XIANG LIN, AND EDWIN A.H. VOLLEBREGT	7 357
A Nonoverlapping Subdomain Algorithm with Lagrange Multipliers and Its Object Oriented Implementation for Interface Problems DAOOL YANG	365
	000
Part 3. Theory	375
A Robin-Robin Preconditioner for an Advection-Diffusion Problem Yves Achdou and Frédéric Nataf	377
A Semi-dual Mode Synthesis Method for Plate Bending Vibrations Frédéric Bourquin and Rabah Namar	384
Overlapping Schwarz Algorithms for Solving Helmholtz's Equation XIAO-CHUAN CAI, MARIO A. CASARIN, FRANK W. ELLIOTT, JR., ANI OLOF B. WIDLUND	) 391
Symmetrized Method with Optimized Second-Order Conditions for the Helmholtz Equation PHILIPPE CHEVALIER AND FRÉDÉRIC NATAF	400
Non-overlapping Schwarz Method for Systems of First Order Equations SÉBASTIEN CLERC	408
Interface Conditions and Non–overlapping Domain Decomposition Methods for a Fluid–Solid Interaction Problem	
XIAOBING FENG	417
Overlapping Schwarz Waveform Relaxation for Parabolic Problems MARTIN J. GANDER	425
Domain Decomposition, Operator Trigonometry, Robin Condition KARL GUSTAFSON	432
On Orthogonal Polynomial Bases for Triangles and Tetrahedra Invariant unde the Symmetric Group	r 420
GARI MAN-KWONG HUI AND HOWARD SWANN	438
On Schwarz Alternating Methods for Nonlinear Elliptic Problems SHIU HONG LUI	447
Convergence Results for Non-Conforming <i>hp</i> Methods: The Mortar Finite Element Method PADMANABHAN SESHAIVER AND MANU SUPL	152
A DEBUG DESIGNATION MAD WANTE DUN	<b>TOO</b>

ix

Intergrid Transfer Operators for Biharmonic Problems Using Nonconforming Plate Elements on Nonnested Meshes	
Zhongci Shi and Zhenghui Xie	460
Additive Schwarz Methods for Hyperbolic Equations Yunhai Wu, Xiao-Chuan Cai, and David E. Keyes	468
Part 4. Applications	477
A Minimum Overlap Restricted Additive Schwarz Preconditioner and Applications in 3D Flow Simulations XIAO-CHUAN CAI, CHARBEL FARHAT, AND MARCUS SARKIS	479
Time Domain Decomposition for European Options in Financial Modelling DIANE CRANN, ALAN J. DAVIES, CHOI-HONG LAI, AND SWEE H. LEONG	486
Parallel Modal Synthesis Methods in Structural Dynamics JEAN-MICHEL CROS	492
Efficient Computation of Aerodynamic Noise Georgi S. Djambazov, Choi-Hong Lai, and Koulis A. Pericleous	500
Non-overlapping Domain Decomposition Applied to Incompressible Flow Problems FRANK-CHRISTIAN OTTO AND GERT LUBE	507
A Domain Decomposition Based Algorithm for Non-linear 2D Inverse Heat Conduction Problems CHARAKA J. PALANSURIYA, CHOI-HONG LAI, CONSTANTINOS S. IEROTHEOU, AND KOULIS A. PERICLEOUS	515
Overlapping Domain Decomposition and Multigrid Methods for Inverse Problems XUE-CHENG TAI, JOHNNY FRØYEN, MAGNE S. ESPEDAL, AND TONY F. CHAN	523
Some Results on Schwarz Methods for a Low–Frequency Approximation of Time–Dependent Maxwell's Equations in Conductive Media ANDREA TOSELLI	530
Parallel Computing for Reacting Flows Using Adaptive Grid Refinement ROBBERT L. VERWEIJ, ARIS TWERDA, AND TIM W.J. PEETERS	538
The Coupling of Mixed and Conforming Finite Element Discretizations CHRISTIAN WIENERS AND BARBARA I. WOHLMUTH	547

### Preface

The annual International Conference on Domain Decomposition Methods for Partial Differential Equations has been a major event in Applied Mathematics and Engineering for the last ten years. The proceedings of the Conferences have become a standard reference in the field, publishing seminal papers as well as the latest theoretical results and reports on practical applications.

The Tenth Conference on Domain Decomposition Methods took place at the University of Colorado at Boulder from August 10 to August 14, 1997. It was organized by Charbel Farhat, Department of Aerospace Engineering Science, Xiao-Chuan Cai, Department of Computer Science, both at the University of Colorado at Boulder, and Jan Mandel, Department of Mathematics at the University of Colorado at Denver.

Driven by the availability of powerful parallel processors, the field of Domain Decomposition has matured during the past ten years. The focus of new methods has been shifting from positive definite elliptic problems to complicated applications, nonlinear problems, systems, and problems with non-elliptic numerical behavior, such as wave propagation and the Helmholtz equation. At the same time, the advent of practical massively parallel computers poses new challenges for elliptic equations, especially on arbitrary, nonuniform meshes. These Proceedings contain contributions from all these areas. The focus of the Conference, as reflected in the selection of invited speakers, was on realistic applications in structural mechanics, structural dynamics, computational fluid dynamics, and heat transfer.

The Conference had 171 registered participants. There were 16 invited plenary lectures and 113 mini-symposia and plenary presentations. These proceedings contain 13 invited and 41 mini-symposia and contributed papers. All papers have been refereed. The Proceedings are divided into four parts. The first part contains invited papers. The rest of the volume contains mini-symposia and contributed presentations, further divided into Algorithms, Theory, and Applications.

Previous proceedings of the International Conferences on Domain Decomposition were published by SIAM, AMS, and John Wiley & Sons. We welcome the return of the Proceedings to AMS. We would like to acknowledge the help of the AMS staff in deciding the format and preparing the Proceedings. We would like to thank particularly Dr. Sergei Gelfand for encouraging us to abolish the page limit for invited presentations.

We wish to thank the members of the International Scientific Committee, and in particular the Chair, Petter Bjørstad, for their help in setting the scientific direction of the Conference. We are also grateful to the organizers of the mini-symposia for attracting high-quality presentations.

#### PREFACE

Timely production of these Proceedings would not have been possible without the cooperation of the authors and the anonymous referees. We would like to thank them all for their graceful and timely response to our various demands.

The organizers of the Conference would like to acknowledge the sponsors of the Conference, namely the National Science Foundation, ANSYS, Inc., the Sandia National Laboratories, the Colorado School of Mines, the University of Colorado at Boulder, and the University of Colorado at Denver. Their generous support made the Conference possible and, among other things, allowed the organizers to fund the participation of graduate students.

Finally, we would like to express our appreciation to Ms. Cathy Moser, the Secretary of the Conference, who made all organizational details run smoothly, and Dr. Radek Tezaur, the Technical Editor of these Proceedings, who finalized the formatting of the papers in AMS-IATEX and prepared the whole book for printing.

The complete program of the Conference is available at the Conference Web site http://www-math.cudenver.edu/dd10. More related information, including links to other Domain Decomposition conferences and books, can be found at the Official Domain Decomposition Web site at http://www.ddm.org. The purchaser of this volume is entitled to the online edition of this book by AMS. To gain access, follow the instructions given on the form found in the back of this volume.

> Jan Mandel Charbel Farhat Xiao-Chuan Cai

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(Continued from the front of this publication)

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#### **Domain Decomposition Methods 10**

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This volume is divided into four parts: the first part contains invited papers (some of which survey developments over the past decade), and the other parts gather material from mini-symposia and contributed presentations under three headings: Algorithms, Theory, and Applications.



