# **CONTEMPORARY MATHEMATICS**

### 325

# Combinatorial and Geometric Representation Theory

An International Conference on Combinatorial and Geometric Representation Theory October 22–26, 2001 Seoul National University, Seoul, Korea

> Seok-Jin Kang Kyu-Hwan Lee Editors



American Mathematical Society

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This volume represents the proceedings of an international conference on Combinatorial and Geometric Representation Theory that was held at Seoul National University, Seoul, Korea, from October 22–26, 2001.

2000 Mathematics Subject Classification. Primary 05Exx, 14Lxx, 16Gxx, 17Bxx, 20Cxx, 20Gxx, 81Rxx.

#### Library of Congress Cataloging-in-Publication Data

Combinatorial and geometric representation theory : an international conference on combinatorial and geometric representation theory, October 22–26, 2001, Seoul National University, Seoul, Korea / Seok-Jin Kang, Kyu-Hwan Lee, editors.

p. cm. — (Contemporary mathematics, ISSN 0271-4132; 325)

Includes bibliographical references.

ISBN 0-8218-3212-3 (alk. paper)

1. Representations of groups—Congresses. 2. Representations of algebras—Congresses. 3. Combinatorial analysis—Congresses. 4. Geometry—Congresses. I. Kang, Seok-Jin. II. Lee, Kyu-Hwan, 1970— III. Contemporary mathematics (American Mathematical Society); v. 325.

QA176.C66 2001 512'.2—dc21

2002041753

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 $10 \ 9 \ 8 \ 7 \ 6 \ 5 \ 4 \ 3 \ 2 \ 1 \qquad 08 \ 07 \ 06 \ 05 \ 04 \ 03$ 

#### Contents

Twisted Verma modules and their quantized analogues HENNING HAAHR ANDERSEN	1
On tameness of the Hecke algebras of type $B$ SUSUMU ARIKI	11
Tensor product representations of Temperley-Lieb algebras and their centralizer algebras GEORGIA BENKART AND DONGHO MOON	31
The restricted nullcone Jon F. Carlson, Zongzhu Lin, Daniel K. Nakano, and Brian J. Parshall	51
Projective embeddings of varieties of special lattices WILLIAM J. HABOUSH	77
Representations of general linear groups GORDON JAMES	93
Fock space representations for the quantum affine algebra $U_q(C_2^{(1)})$ SEOK-JIN KANG AND JAE-HOON KWON	109
Realizations of crystals Masaki Kashiwara	133
t–analogs of q–characters of quantum affine algebras of type $A_n, D_n$ HIRAKU NAKAJIMA	141
Skew shape representations are irreducible ARUN RAM	161

#### Preface

This volume is the refereed proceedings of the international conference on "Combinatorial and Geometric Representation Theory" that was held at Seoul National University, Seoul, Korea, from October 22nd to October 26th, 2001.

In the area of representation theory, a wide variety of mathematical ideas has been combined together to provide new insights into the field, powerful methods of understanding the theory, and various applications to other branches of mathematics. Over the past two decades, there have been remarkable developments in representation theory based on combinatorial and geometric approaches.

The theme of this conference was to bring together various ideas from combinatorial and geometric aspects of representation theory and discuss the recent developments in this active field of research. We hope this conference served as a good opportunity to understand strong connections between combinatorics, geometry and representation theory.

We are very grateful to all the invited speakers and participants for their excellent lectures, contributed papers and great enthusiasm. We would also like to thank graduate students of Seoul National University for their assistance during the conference. Special thanks should be given to Professors Young-Hyun Cho, Myung-Hwan Kim and In-Sok Lee who served as members of the organizing committee of this conference.

This conference was supported by KOSEF Grant 98-0701-01-5-L. We greatly appreciate their financial and moral support. Finally, we would like to express our gratitude to all the referees for their invaluable help with the contributed papers.

Seok-Jin Kang Kyu-Hwan Lee Editors

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This volume presents the proceedings of the international conference on Combinatorial and Geometric Representation Theory. In the field of representation theory, a wide variety of mathematical ideas are providing new insights, giving powerful methods for understanding the theory, and presenting various applications to other branches of mathematics. Over the past two decades, there have been remarkable developments. This book explains the strong connections between combinatorics, geometry, and representation theory. It is suitable for graduate students and researchers interested in representation theory.



