# CONTEMPORARY MATHEMATICS 

418

## Algebraic Methods in Cryptography

AMS/DMV Joint International Meeting June 16-19, 2005 Mainz, Germany
International Workshop on Algebraic Methods in Cryptography November 17-18, 2005

Bochum, Germany
Lothar Gerritzen
Dorian Goldfeld
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## Preface

This volume consists of contributions by speakers at the Special Session on Algebraic Cryptography at the Joint International Meeting of the AMS with the Deutsche Mathematiker-Vereinigung held in Mainz, Germany, on June 16-19, 2005, and at the International Workshop on Algebraic Methods in Cryptography held in Bochum, Germany, on November 17-18, 2005.

The readers will find here a variety of contributions, mostly related to publickey cryptography, including design of new cryptographic primitives as well as cryptanalysis of previously suggested schemes. Most papers are original research papers in the area that can be loosely defined as "Non-commutative cryptography"; this means that groups (or other algebraic structures) which are used as platforms are non-commutative.

We are grateful to the American Mathematical Society for assisting us in publication of this volume. In particular, we thank Christine M. Thivierge for her patient work in putting this volume together.

Lothar Gerritzen
Dorian Goldfeld
Martin Kreuzer
Gerhard Rosenberger
Vladimir Shpilrain

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