

# Journal of ALGEBRAIC GEOMETRY

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Starting with the 2002 subscription, the *Journal of Algebraic Geometry* is available in both electronic and paper delivery. List price is US\$458 for electronic + paper delivery, US\$424 for electronic only; the price for individuals is US\$190 for electronic + paper delivery, US\$168 for electronic only. If ordering the paper version, add US\$6 for delivery within the United States, US\$13 for delivery outside the United States. Subscription renewals are subject to late fees. See [www.ams.org/journal-faq](http://www.ams.org/journal-faq) for more information.

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This journal is indexed in *Science Citation Index<sup>TM</sup>-Expanded*, *ISI Alerting Services<sup>SM</sup>*, *CompuMath Citation Index<sup>®</sup>*, *Current Contents<sup>®</sup>/Physical, Chemical & Earth Sciences*.

ISSN 1056-3911 (print); ISSN 1534-7486 (online)

Printed in the United States of America.

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- [2] N. Hochster and J. L. Roberts, *Rings of invariants of reductive groups acting on regular rings are Cohen-Macaulay*, *Adv. Math.* **13** (1974) 115–175.

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1056-3911(201804)27:2;1-0