Professor Bernstein places the emphasis on those problems that were not discussed in the above mentioned monograph. He studies in particular the determination of the successive terms in the asymptotic development of the best approximation and the problem of the best approximation to a function having an essentially singular point. This latter is a problem of unusual difficulty, and it is noteworthy that in a wide variety of cases a solution of the problem can be obtained by the use of the same methods as in the case of polar singularities.

The book closes with two notes. The first one, which is rather extensive, develops certain interesting relationships between the problem of analytic extension of analytic functions of real variables and that of polynomial approximation to such functions. The second note, which is brief, deals with a property of analytic functions of genre zero.

As a whole the book has to a very great extent that admirable characteristic of the Borel series: namely, that its interest lies not only in the topics specifically treated, but also in the variety of problems for further research that are either definitely indicated or incidentally suggested.

C. N. Moore


The two volumes give a brief introduction to the theory of the various potentials in two and three dimensional space and to the two boundary value problems. The theorems and methods are in general well known. The author has attempted to reduce the necessary preparation of the reader to a minimum. A knowledge of the calculus is sufficient except in the case of the chapter on the Fredholm equation. After a short mengentheoretische introduction, the first volume takes up the definition and some properties of volume, surface, and double layer potentials. It is shown that the definition of the potential as a solution of Laplace's equation is coextensive with the usual integral definition. This new definition necessitates a new definition of mass and in this the author follows Plemelj. After a chapter on the necessary variations of Stokes' Theorem, the volume closes with a discussion of the continuity properties of the potentials and their derivatives. In the first part of the second volume the author confines himself chiefly to a statement of the Dirichlet and Neumann problems, their solution for the circle and sphere and a discussion of the Green's function. No mention is made of the method of Neumann or of the method of balayage of Poincaré. The remainder of the volume is given over to the theory of Fredholm's equation and its application to the boundary value problems. The chapter on the Fredholm equation is rather too brief to be useful to one who knows nothing of the theory. The work is carefully written and though very concise, is readable and is to be recommended.

C. A. Shook