



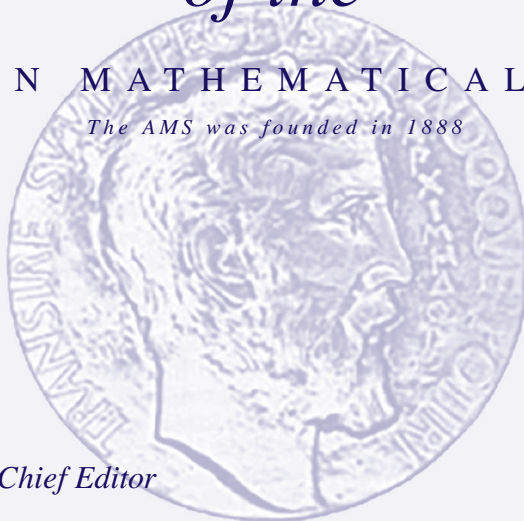
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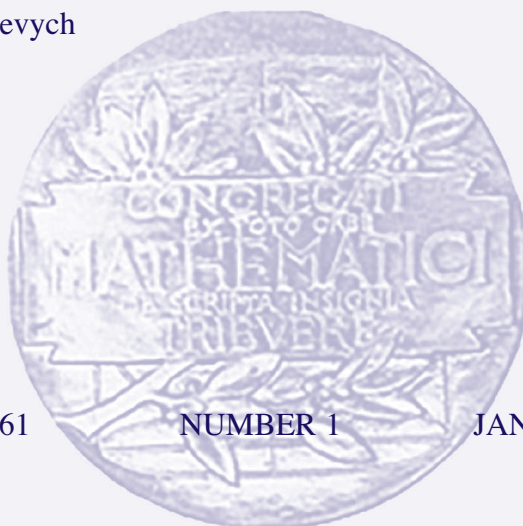
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Articles

Susan Friedlander, *Chief Editor*

Book Reviews

Volodymyr Nekrashevych



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