

# Mathematical Tables *and other* Aids to Computation

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A Quarterly Journal edited on behalf of the  
Committee on Mathematical Tables  
and Other Aids to Computation

by

RAYMOND CLARE ARCHIBALD  
DERRICK HENRY LEHMER

WITH THE COÖPERATION OF

LESLIE JOHN COMRIE  
SOLOMON ACHILLOVICH JOFFE

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