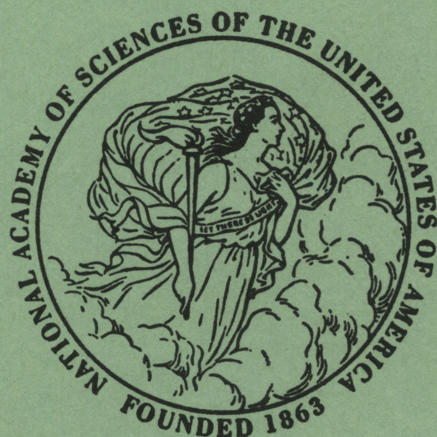


*Volume X*

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# Mathematical Tables *and other* Aids to Computation



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# Mathematical Tables *and other* Aids to Computation

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