

PROCEEDINGS  
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AMERICAN MATHEMATICAL SOCIETY

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I. M. SHEFFER

MAX SHIFFMAN

G. W. WHITEHEAD

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## Journals Published by the American Mathematical Society

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