Thus we can easily obtain the following metric characterization, instead of (20), of the invariant $J$ given by equation (19):

$$J = \left( \frac{2 \sin \omega}{3 \sin \theta} \right)^6 \frac{R^2 R^4}{T^6 T}.$$