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The current issue of the journal lists editors to whom prospective publications should be addressed. Publication is bimonthly.

Transactions of the American Mathematical Society. This monthly journal is devoted entirely to research in pure and applied mathematics, and includes in general longer papers than those in the PROCEEDINGS.

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Mathematical Reviews. This journal is devoted to abstracts and reviews of the current mathematical literature of the world. Currently publication is monthly; two volumes are published each year, each volume consisting of 6 regular issues plus an index issue. In each regular issue the abstracts and reviews are grouped under subject headings. Publication began in 1940.

Soviet Mathematics—Doklady. This bimonthly is a translation journal containing the entire pure mathematics section of the DOKLADY AKADEMII NAUK SSSR, the Reports of the Academy of Sciences of the USSR. The DOKLADY for a year contains about 500 articles, each about 4 pages long.

Mathematics of the USSR—Izvestija. This journal is a cover-to-cover translation of IZVESTIJA AKADEMII NAUK SSSR SERIJA MATEMATICHESKAYA, published bimonthly by the Academy of Sciences of the USSR. It is a journal of current research in all fields of pure mathematics.

Mathematics of the USSR—Sbornik. This journal is a cover-to-cover translation of MATEMATICHESKIĬ SBORNIK (New Series), published monthly by the Moscow Mathematical Society and the Academy of Sciences of the USSR. It is a journal of current research in all fields of pure mathematics.

Theory of Probability and Mathematical Statistics. This journal is the cover-to-cover translation of the Teoriya Verojatnostei i Matematicheskaja Statistika published by Kiev University, beginning with the 1970 Soviet publication.

Vestnik of the Leningrad University (Mathematics). This is the complete translation of the mathematics section of the Vestnik Leningradskogo Universiteta, beginning with the Soviet publication of 1968. All fields of mathematics are covered.

Current Mathematical Publications (formerly Contents of Contemporary Mathematical Journals and New Publications). This is issued bi-weekly and contains a subject-classified index of papers and books being published currently in mathematics.

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Send papers directly to one of the editors listed under the subject field of the paper. The numbers in parentheses are the first two digits of major classifications from the AMS (MOS) Subject Classification Scheme (1970) and describes the fields being handled by the editor.

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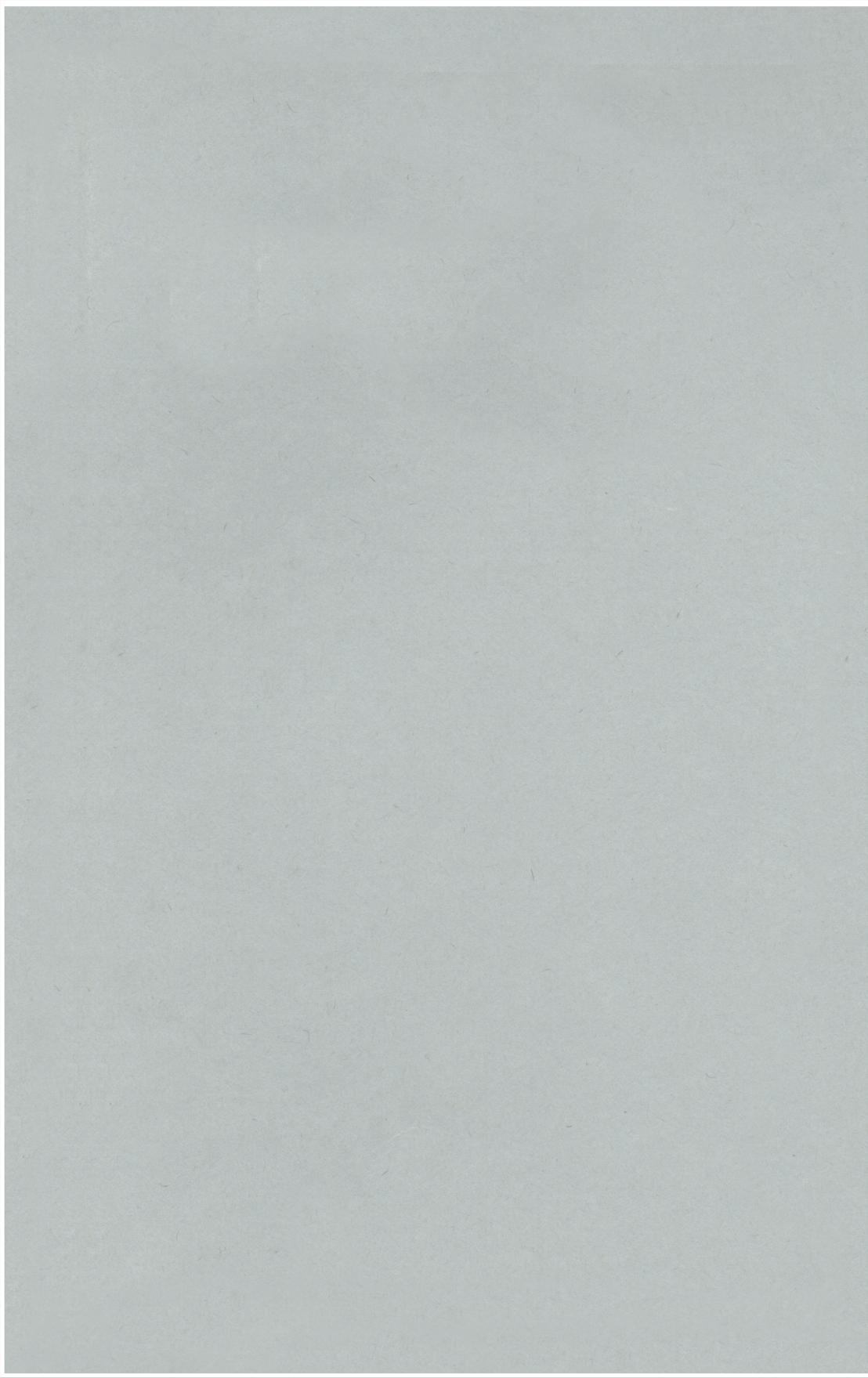
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