

ERRATUM TO “DIRICHLET BOUNDARY CONDITIONS FOR  
ELLIPTIC OPERATORS WITH UNBOUNDED DRIFT”

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The statement of Theorem 2.4 in our paper published in vol. 133, no. 9 (2005), pages 2625–2635, must be changed as follows.

**Theorem 2.4.** *Let  $\Phi$  be a  $C^2$  function such that  $\Phi(x) + \alpha|x|^2/2$  is convex for some  $\alpha > 0$ , assume that  $\partial\Omega \in C^3$  and that*

$$\frac{\partial\Phi}{\partial n} - H \leq 0.$$

*Then  $(A, D(A))$  is self-adjoint and dissipative in  $L^2(\Omega, \mu)$ . Moreover, the map  $u \mapsto \langle (D^2\Phi)Du, Du \rangle$  is continuous from  $D(A)$  to  $L^1(\Omega, \mu)$ .*

Here  $H = H(x)$  is the scalar mean curvature of  $\partial\Omega$  at  $x$ , taken positive if  $\Omega$  is convex.

The proof remains the same except at one point; at the beginning of page 2629 we have to use the identity

$$\Delta u = \langle (D^2u)n, n \rangle + H \frac{\partial u}{\partial n} \text{ at } \partial\Omega$$

for regular functions  $u$  vanishing at  $\partial\Omega$ , instead of  $\Delta u = \langle (D^2u)n, n \rangle$ . Accordingly, from the equality  $\lambda u - \mathcal{A}u = f$  at  $\partial\Omega$  we get the estimate

$$\int_{\partial\Omega} \theta_R^2 \langle (D^2u)n, Du \rangle e^{-\Phi} d\sigma \leq \int_{\partial\Omega} \theta_R^2 \left( \frac{\partial\Phi}{\partial n} - H \right) \left( \frac{\partial u}{\partial n} \right)^2 e^{-\Phi} d\sigma$$

instead of

$$\int_{\partial\Omega} \theta_R^2 \langle (D^2u)n, Du \rangle e^{-\Phi} d\sigma \leq \int_{\partial\Omega} \theta_R^2 \frac{\partial\Phi}{\partial n} \left( \frac{\partial u}{\partial n} \right)^2 e^{-\Phi} d\sigma.$$

Theorem 2.5 holds without any change in the statement because if  $\partial\Omega$  is uniformly  $C^2$ , then  $H$  is bounded.

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