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(Formerly Leningrad Mathematical Journal)

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Volume 18 Number 1 2007

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*A Translation of*

РОССИЙСКАЯ АКАДЕМИЯ НАУК

## АЛГЕБРА И АНАЛИЗ

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“Наука”, С.-Петербургское отделение, 2006 г.

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