

# St. Petersburg Mathematical Journal

(Formerly Leningrad Mathematical Journal)

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Volume 20 Number 5 October 2009

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РОССИЙСКАЯ АКАДЕМИЯ НАУК

## АЛГЕБРА И АНАЛИЗ

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