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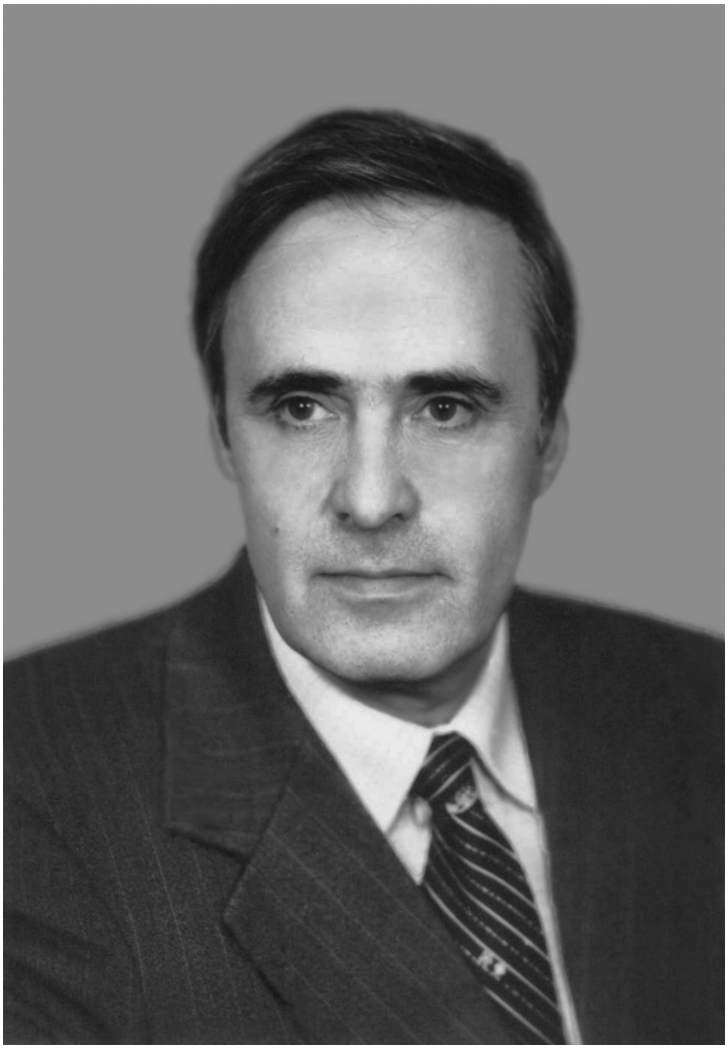

This issue is dedicated to the memory
of our teacher and colleague
Mikhail Shlëmovich Birman,
an outstanding mathematician
and a remarkable person.

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