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РОССИЙСКАЯ АКАДЕМИЯ НАУК

АЛГЕБРА

И

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Алгебра и анализ

“Наука”, С.-Петербургское отделение, 2020 г.

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