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A M E R I C A N M A T H E M A T I C A L S O C I E T Y

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A Translation of

数 学



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AMERICAN  
MATHEMATICAL  
SOCIETY

Providence, Rhode Island USA

# Sugaku Expositions

*A translation of the expository articles of*

# 数 学

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