
VOLUME 363 NUMBER 1



JANUARY 2011

WHOLE NUMBER 908

TRANSACTIONS

OF THE

A M E R I C A N M A T H E M A T I C A L S O C I E T Y

EDITED BY

Dan Abramovich
Alejandro Adem
Luchezar L. Avramov
Erik van den Ban
Richard F. Bass
Mark Feighn
Robert Guralnick, Managing Editor
Yunping Jiang
Alexander Kleshchev
Steffen Lempert
William P. Minicozzi II
Alexander Nagel
Peter Polacik
Gustavo Ponce
Jonathan Rogawski
Shankar Sen
Dimitri Shlyakhtenko
John R. Stembridge
Daniel Tataru
Mina Teicher
Chris Woodward

PROVIDENCE, RHODE ISLAND USA

ISSN 0002-9947

Available electronically at
www.ams.org/tran/

Transactions of the American Mathematical Society

This journal is devoted entirely to research in pure and applied mathematics.

Submission information. See **Information for Authors** at the end of this issue.

Publisher Item Identifier. The Publisher Item Identifier (PII) appears at the top of the first page of each article published in this journal. This alphanumeric string of characters uniquely identifies each article and can be used for future cataloging, searching, and electronic retrieval.

Postings to the AMS website. Articles are posted to the AMS website individually after proof is returned from authors and before appearing in an issue.

Subscription information. *Transactions of the American Mathematical Society* is published monthly and is also accessible electronically from www.ams.org/journals/. Subscription prices for Volume 363 (2011) are as follows: for paper delivery, US\$1991 list, US\$1592.80 institutional member, US\$1791.90 corporate member; for electronic delivery, US\$1792 list, US\$1433.60 institutional member, US\$1612.80 corporate member. Upon request, subscribers to paper delivery of this journal are also entitled to receive electronic delivery. If ordering the paper version, add US\$81 for surface delivery outside the United States and India; US\$114 to India. Expedited delivery to destinations in North America is US\$89; elsewhere US\$240. Subscription renewals are subject to late fees. See www.ams.org/help-faq for more journal subscription information.

Back number information. For back issues see www.ams.org/bookstore.

Subscriptions and orders should be addressed to the American Mathematical Society, P.O. Box 845904, Boston, MA 02284-5904 USA. *All orders must be accompanied by payment.* Other correspondence should be addressed to 201 Charles Street, Providence, RI 02904-2294 USA.

Copying and reprinting. Material in this journal may be reproduced by any means for educational and scientific purposes without fee or permission with the exception of reproduction by services that collect fees for delivery of documents and provided that the customary acknowledgment of the source is given. This consent does not extend to other kinds of copying for general distribution, for advertising or promotional purposes, or for resale. Requests for permission for commercial use of material should be addressed to the Acquisitions Department, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA. Requests can also be made by e-mail to reprint-permission@ams.org.

Excluded from these provisions is material in articles for which the author holds copyright. In such cases, requests for permission to use or reprint should be addressed directly to the author(s). (Copyright ownership is indicated in the notice in the lower right-hand corner of the first page of each article.)

Transactions of the American Mathematical Society (ISSN 0002-9947) is published monthly by the American Mathematical Society at 201 Charles Street, Providence, RI 02904-2294 USA. Periodicals postage is paid at Providence, Rhode Island. Postmaster: Send address changes to *Transactions*, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA.

© 2011 by the American Mathematical Society. All rights reserved.

This journal is indexed in *Mathematical Reviews*, *Zentralblatt MATH*, *Science Citation Index*[®], *Science Citation Index*TM-*Expanded*, *ISI Alerting Services*SM, *CompuMath Citation Index*[®], and *Current Contents*[®]/*Physical, Chemical & Earth Sciences*. This journal is archived in *Portico*.

Printed in the United States of America.

⊗ The paper used in this journal is acid-free and falls within the guidelines established to ensure permanence and durability.

TRANSACTIONS OF THE AMERICAN MATHEMATICAL SOCIETY

CONTENTS

Vol. 363, No. 1

Whole No. 908

January 2011

Filippo Morabito , <i>A Costa-Hoffman-Meeks type surface in $\mathbb{H}^2 \times \mathbb{R}$</i>	1
Dimitar Vassilev , <i>L^p estimates and asymptotic behavior for finite energy solutions of extremals to Hardy-Sobolev inequalities</i>	37
Mohammad Ghomi and Robert E. Greene , <i>Relative isometric embeddings of Riemannian manifolds</i>	63
Thomas Foerstersch and Katrin Radke , <i>Characterizing complete $\text{CAT}(\kappa)$-spaces, $\kappa < 0$, with geodesic boundary</i>	75
Kjetil Røysland , <i>Frames generated by actions of countable discrete groups</i>	95
M. Grau, F. Mañosas, and J. Villadelprat , <i>A Chebyshev criterion for Abelian integrals</i>	109
Matthew Dulock and Min Ru , <i>Uniqueness of holomorphic curves into abelian varieties</i>	131
Bruce Solomon , <i>X-rays of forms and projections of currents</i>	143
Sebastian Goette , <i>Scalar curvature estimates by parallel alternating torsion</i>	165
Paulo A. S. Caetano and Paulo D. Cordaro , <i>Gevrey solvability and Gevrey regularity in differential complexes associated to locally integrable structures</i>	185
Lasse Rempe and Sebastian van Strien , <i>Absence of line fields and Mañé's theorem for nonrecurrent transcendental functions</i>	203
Juan C. Migliore, Rosa M. Miró-Roig, and Uwe Nagel , <i>Monomial ideals, almost complete intersections and the Weak Lefschetz property</i>	229
Sangbum Cho and Darryl McCullough , <i>Tunnel leveling, depth, and bridge numbers</i>	259
Eberhard Freitag and Riccardo Salvati Manni , <i>The modular variety of hyperelliptic curves of genus three</i>	281
Johannes Jaerisch and Marc Kesseböhmer , <i>Regularity of multifractal spectra of conformal iterated function systems</i>	313
Hiroyuki Inou , <i>Extending local analytic conjugacies</i>	331
David P. Blecher and Upasana Kashyap , <i>A characterization and a generalization of W^*-modules</i>	345
Přemysl Jedlička, Michael Kinyon, and Petr Vojtěchovský , <i>The structure of commutative automorphic loops</i>	365
Richard Scott , <i>Rationality and reciprocity for the greedy normal form of a Coxeter group</i>	385
V. V. Bavula , <i>Extensions of the Frobenius to the ring of differential operators on a polynomial algebra in prime characteristic</i>	417
Amanda Folsom , <i>Kac-Wakimoto characters and universal mock theta functions</i>	439
Susan J. Sierra , <i>Geometric idealizer rings</i>	457
Christina Brech and Piotr Koszmider , <i>Thin-very tall compact scattered spaces which are hereditarily separable</i>	501

Victor Reiner, Alexander Woo, and Alexander Yong, Presenting the cohomology of a Schubert variety	521
Dariusz Cichoń, Jan Stochel, and Franciszek Hugon Szafraniec, Extending positive definiteness	545

Editorial Information

To be published in the *Transactions*, a paper must be correct, new, nontrivial, and significant. Further, it must be well written and of interest to a substantial number of mathematicians. Piecemeal results, such as an inconclusive step toward an unproved major theorem or a minor variation on a known result, are in general not acceptable for publication.

Papers submitted to the *Transactions* should be 15 or more published journal pages in length. Shorter papers may be submitted to the *Proceedings of the American Mathematical Society*. Published pages are the same size as those generated in the style files provided for $\mathcal{A}\mathcal{M}\mathcal{S}$ - $\mathcal{L}\mathcal{A}\mathcal{T}\mathcal{E}\mathcal{X}$ or $\mathcal{A}\mathcal{M}\mathcal{S}$ - $\mathcal{T}\mathcal{E}\mathcal{X}$.

Information on the backlog for this journal can be found on the AMS website starting from <http://www.ams.org/tran>.

In an effort to make articles available as quickly as possible, articles are posted to the AMS website individually after proof is returned from authors and before appearing in an issue.

A Consent to Publish and Copyright Agreement is required before a paper will be published in this journal. After a paper is accepted for publication, the Providence office will send a Consent to Publish and Copyright Agreement to all authors of the paper. By submitting a paper to this journal, authors certify that the results have not been submitted to nor are they under consideration for publication by another journal, conference proceedings, or similar publication.

Information for Authors

Initial submission. The AMS uses Centralized Manuscript Processing for initial submissions. Authors should submit a PDF file using the Initial Manuscript Submission form found at www.ams.org/submission/tran, or send one copy of the manuscript to the following address: Centralized Manuscript Processing, TRANSACTIONS OF THE AMS, 201 Charles Street, Providence, RI 02904-2294 USA. If a paper copy is being forwarded to the AMS, indicate that it is for *Transactions* and include the name of the corresponding author, contact information such as email address or mailing address, and the name of an appropriate Editor to review the paper (see the list of Editors below).

The first page of an article must consist of a *descriptive title*, followed by an *abstract* that summarizes the article in language suitable for workers in the general field (algebra, analysis, etc.). The *descriptive title* should be short, but informative; useless or vague phrases such as “some remarks about” or “concerning” should be avoided. The *abstract* should be at least one complete sentence, and at most 300 words. Included with the footnotes to the paper should be the 2010 *Mathematics Subject Classification* representing the primary and secondary subjects of the article. The classifications are accessible from www.ams.org/msc/. The Mathematics Subject Classification footnote may be followed by a list of *key words and phrases* describing the subject matter of the article and taken from it. Journal abbreviations used in bibliographies are listed in the latest *Mathematical Reviews* annual index. The series abbreviations are also accessible from www.ams.org/msnhtml/serials.pdf. To help in preparing and verifying references, the AMS offers MR Lookup, a Reference Tool for Linking, at www.ams.org/mrlookup/.

Electronically prepared manuscripts. The AMS encourages electronically prepared manuscripts, with a strong preference for $\mathcal{A}\mathcal{M}\mathcal{S}$ - $\mathcal{L}\mathcal{A}\mathcal{T}\mathcal{E}\mathcal{X}$. To this end, the Society has prepared $\mathcal{A}\mathcal{M}\mathcal{S}$ - $\mathcal{L}\mathcal{A}\mathcal{T}\mathcal{E}\mathcal{X}$ author packages for each AMS publication. Author packages include instructions for preparing electronic manuscripts, samples,

and a style file that generates the particular design specifications of that publication series. Articles properly prepared using the $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX style file and the $\backslash\text{label}$ and $\backslash\text{ref}$ commands automatically enable extensive intra-document linking to the bibliography and other elements of the article for searching electronically on the Web. Because linking must often be added manually to electronically prepared manuscripts in other forms of \TeX , using $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX also reduces the amount of technical intervention once the files are received by the AMS. This results in fewer errors in processing and saves the author proofreading time. $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX papers also move more efficiently through the production stream, helping to minimize publishing costs.

$\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX is the highly preferred format of \TeX , but author packages are also available in $\mathcal{A}\mathcal{M}\mathcal{S}$ - \TeX . Those authors who make use of these style files from the beginning of the writing process will further reduce their own efforts. Manuscripts prepared electronically in \LaTeX or plain \TeX are normally not acceptable due to the high amount of technical time required to insure that the file will run properly through the AMS in-house production system. \LaTeX users will find that $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX is the same as \LaTeX with additional commands to simplify the typesetting of mathematics, and users of plain \TeX should have the foundation for learning $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX .

Authors may retrieve an author package for *Transactions of the AMS* from www.ams.org/tran/tranauthorpac.html or via FTP to [ftp.ams.org](ftp://ftp.ams.org) (login as **anonymous**, enter your complete email address as password, and type **cd pub/author-info**). The *AMS Author Handbook* and the *Instruction Manual* are available in PDF format from the author package link. The author package can also be obtained free of charge by sending email to tech-support@ams.org, or from the Publication Division, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA. When requesting an author package, please specify $\mathcal{A}\mathcal{M}\mathcal{S}$ - \LaTeX or $\mathcal{A}\mathcal{M}\mathcal{S}$ - \TeX and the publication in which your paper will appear. Please be sure to include your complete email address.

After acceptance. The source files for the final version of the electronic manuscript should be sent to the Providence office immediately after the paper has been accepted for publication. The author should also submit a PDF of the final version of the paper to the Editor, who will forward a copy to the Providence office. Accepted electronically prepared manuscripts can be submitted via the web at www.ams.org/submit-book-journal/, sent via email to pub-submit@ams.org, or sent on CD to the Electronic Prepress Department, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA. When sending a manuscript electronically via email or CD, please be sure to include a message indicating in which publication the paper has been accepted. No corrections will be accepted electronically. Authors must mark their changes on their proof copies and return them to the Providence office. Complete instructions on how to send files are included in the author package.

Electronic graphics. Comprehensive instructions on preparing graphics are available starting from www.ams.org/authors/journals.html. A few of the major requirements are given here.

Submit files for graphics as EPS (Encapsulated PostScript) files. This includes graphics originated via a graphics application as well as scanned photographs or other computer-generated images. If this is not possible, TIFF files are acceptable as long as they can be opened in Adobe Photoshop or Illustrator.

Authors using graphics packages for the creation of electronic art should also avoid the use of any lines thinner than 0.5 points in width. Many graphics packages

allow the user to specify a “hairline” for a very thin line. Hairlines often look acceptable when proofed on a typical laser printer. However, when produced on a high-resolution laser imagesetter, hairlines become nearly invisible and will be lost entirely in the final printing process.

Screens should be set to values between 15% and 85%. Screens which fall outside of this range are too light or too dark to print correctly. Variations of screens within a graphic should be no less than 10%.

AMS policy on making changes to articles after posting. Articles are posted to the AMS website individually after proof is returned from authors and before appearing in an issue. To preserve the integrity of electronically published articles, once an article is individually posted to the AMS website but not yet in an issue, changes cannot be made in place in the paper. However, an “Added after posting” section may be added to the paper right before the References when there is a critical error in the content of the paper. The “Added after posting” section gives the author an opportunity to correct this type of critical error before the article is put into an issue for printing and before it is then reposted with the issue. The “Added after posting” section remains a permanent part of the paper. The AMS does not keep author-related information, such as affiliation, current address, and email address, up to date after a paper is initially posted.

Once the article is assigned to an issue, even if the issue has not yet been posted to the AMS website, corrections may be made to the paper by submitting a traditional errata article. The errata article will appear in a future print issue and will link back and forth on the web to the original article online.

Secure manuscript tracking on the Web. Authors can track their manuscripts through the AMS journal production process using the personal AMS ID and Article ID printed in the upper right-hand corner of the Consent to Publish form sent to each author who publishes in AMS journals. Access to the tracking system is available from www.ams.org/mstrack/. An explanation of each production step is provided on the web through links from the manuscript tracking screen. Questions can be sent to tran-query@ams.org.

Inquiries. Any inquiries concerning a paper that has been accepted for publication that cannot be answered via the manuscript tracking system mentioned above should be sent to tran-query@ams.org or directly to the Electronic Prepress Department, American Mathematical Society, 201 Charles Street, Providence, RI 02904-2294 USA.

Editors

The AMS uses Centralized Manuscript Processing for initial submissions to AMS journals. Authors should follow instructions listed on the Initial Submission page found at www.ams.org/tran/transubmit.html.

Algebra, ALEXANDER KLESHCHEV, Department of Mathematics, University of Oregon, Eugene, OR 97403-1222 USA; e-mail: klesh@uoregon.edu

Algebraic geometry, DAN ABRAMOVICH, Department of Mathematics, Brown University, Box 1917, Providence, RI 02912 USA; e-mail: amsedit@math.brown.edu

Algebraic geometry and its applications, MINA TEICHER, Emmy Noether Research Institute for Mathematics, Bar-Ilan University, Ramat-Gan 52900, Israel; e-mail: teicher@macs.biu.ac.il

Algebraic topology, ALEJANDRO ADEM, Department of Mathematics, University of British Columbia, Room 121, 1984 Mathematics Road, Vancouver, British Columbia, Canada V6T 1Z2; e-mail: transactions@math.ubc.ca

Combinatorics, JOHN R. STEMBRIDGE, Department of Mathematics, University of Michigan, Ann Arbor, MI 48109-1043 USA; e-mail: jrs@umich.edu

Commutative and homological algebra, LUCHEZAR L. AVRAMOV, Department of Mathematics, University of Nebraska, Lincoln, NE 68588-0130 USA; e-mail: avramov@math.unl.edu

Complex analysis and harmonic analysis, ALEXANDER NAGEL, Department of Mathematics, University of Wisconsin, 480 Lincoln Drive, Madison, WI 53706-1313 USA; e-mail: nagel@math.wisc.edu

Differential geometry and global analysis, CHRIS WOODWARD, Department of Mathematics, Rutgers University, 110 Frelinghuysen Road, Piscataway, NJ 08854 USA; e-mail: ctw@rutgers.edu

Dynamical systems and ergodic theory and complex analysis, YUNPING JIANG, Department of Mathematics, CUNY Queens College and Graduate Center, 65-30 Kissena Boulevard, Flushing, NY 11367 USA; e-mail: yuping.jiang@qc.cuny.edu

Functional analysis and operator algebras, DIMITRI SHLYAKHTENKO, Department of Mathematics, University of California, Los Angeles, CA 90095 USA; e-mail: shlyakht@math.ucla.edu

Geometric analysis, WILLIAM P. MINICOZZI II, Department of Mathematics, Johns Hopkins University, 3400 N. Charles Street, Baltimore, MD 21218 USA; e-mail: trans@math.jhu.edu

Geometric topology, MARK FEIGN, Department of Mathematics, Rutgers University, Newark, NJ 07102 USA; e-mail: feighn@andromeda.rutgers.edu

Harmonic analysis, representation theory, and Lie theory, ERIK VAN DEN BAN, Department of Mathematics, Utrecht University, P.O. Box 80 010, 3508 TA Utrecht, The Netherlands; e-mail: E.P.vandenBan@uu.nl

Logic, STEFFEN LEMPP, Department of Mathematics, University of Wisconsin, 480 Lincoln Drive, Madison, WI 53706-1388 USA; e-mail: lempp@math.wisc.edu

Number theory, JONATHAN ROGAWSKI, Department of Mathematics, University of California, Los Angeles, CA 90095 USA; e-mail: jonr@math.ucla.edu

Number theory, SHANKAR SEN, Department of Mathematics, 505 Malott Hall, Cornell University, Ithaca, NY 14853 USA; e-mail: ss70@cornell.edu

Partial differential equations, GUSTAVO PONCE, Department of Mathematics, South Hall, Room 6607, University of California, Santa Barbara, CA 93106 USA; e-mail: ponce@math.ucsb.edu

Partial differential equations and dynamical systems, PETER POLACIK, School of Mathematics, University of Minnesota, Minneapolis, MN 55455 USA; e-mail: polacik@math.umn.edu

Probability and statistics, RICHARD F. BASS, Department of Mathematics, University of Connecticut, Storrs, CT 06269-3009 USA; e-mail: bass@math.uconn.edu

Real analysis and partial differential equations, DANIEL TATARU, Department of Mathematics, University of California, Berkeley, CA 94720 USA; e-mail: tataru@math.berkeley.edu

All other communications to the editors should be addressed to the Managing Editor, ROBERT GURALNICK, Department of Mathematics, University of Southern California, Los Angeles, CA 90089-1113 USA; e-mail: guralnic@math.usc.edu

MEMOIRS OF THE AMERICAN MATHEMATICAL SOCIETY

Memoirs is devoted to research in pure and applied mathematics of the same nature as *Transactions*. An issue consists of one or more separately bound research tracts for which the authors provide reproduction copy. Papers intended for *Memoirs* should normally be at least 80 pages in length. *Memoirs* has the same editorial committee as *Transactions*; authors may choose an Editor from the list above upon submission.

(Continued from back cover)

Amanda Folsom , Kac-Wakimoto characters and universal mock theta functions	439
Susan J. Sierra , Geometric idealizer rings	457
Christina Brech and Piotr Koszmider , Thin-very tall compact scattered spaces which are hereditarily separable	501
Victor Reiner, Alexander Woo, and Alexander Yong , Presenting the cohomology of a Schubert variety	521
Dariusz Cichoń, Jan Stochel, and Franciszek Hugon Szafraniec , Extending positive definiteness	545

TRANSACTIONS OF THE AMERICAN MATHEMATICAL SOCIETY
 CONTENTS

Vol. 363, No. 1

Whole No. 908

January 2011

Filippo Morabito, <i>A Costa-Hoffman-Meeks type surface in $\mathbb{H}^2 \times \mathbb{R}$</i>	1
Dimitar Vassilev, <i>L^p estimates and asymptotic behavior for finite energy solutions of extremals to Hardy-Sobolev inequalities</i>	37
Mohammad Ghomi and Robert E. Greene, <i>Relative isometric embeddings of Riemannian manifolds</i>	63
Thomas Foertsch and Katrin Radke, <i>Characterizing complete $CAT(\kappa)$-spaces, $\kappa < 0$, with geodesic boundary</i>	75
Kjetil Røysland, <i>Frames generated by actions of countable discrete groups</i>	95
M. Grau, F. Mañosas, and J. Villadelprat, <i>A Chebyshev criterion for Abelian integrals</i>	109
Matthew Dulock and Min Ru, <i>Uniqueness of holomorphic curves into abelian varieties</i>	131
Bruce Solomon, <i>X-rays of forms and projections of currents</i>	143
Sebastian Goette, <i>Scalar curvature estimates by parallel alternating torsion</i>	165
Paulo A. S. Caetano and Paulo D. Cordaro, <i>Gevrey solvability and Gevrey regularity in differential complexes associated to locally integrable structures</i>	185
Lasse Rempe and Sebastian van Strien, <i>Absence of line fields and Mañé's theorem for nonrecurrent transcendental functions</i>	203
Juan C. Migliore, Rosa M. Miró-Roig, and Uwe Nagel, <i>Monomial ideals, almost complete intersections and the Weak Lefschetz property</i>	229
Sangbum Cho and Darryl McCullough, <i>Tunnel leveling, depth, and bridge numbers</i>	259
Eberhard Freitag and Riccardo Salvati Manni, <i>The modular variety of hyperelliptic curves of genus three</i>	281
Johannes Jaerisch and Marc Kesseböhmer, <i>Regularity of multifractal spectra of conformal iterated function systems</i>	313
Hiroyuki Inou, <i>Extending local analytic conjugacies</i>	331
David P. Blecher and Upasana Kashyap, <i>A characterization and a generalization of W^*-modules</i>	345
Přemysl Jedlička, Michael Kinyon, and Petr Vojtěchovský, <i>The structure of commutative automorphic loops</i>	365
Richard Scott, <i>Rationality and reciprocity for the greedy normal form of a Coxeter group</i>	385
V. V. Bavula, <i>Extensions of the Frobenius to the ring of differential operators on a polynomial algebra in prime characteristic</i>	417

(Continued on inside back cover)



0002-9947(201101)363:1;1-R