

Mathematical Tables *and other* Aids to Computation

A Quarterly Journal edited on behalf of the
Committee on Mathematical Tables
and Other Aids to Computation

by

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DERRICK HENRY LEHMER

WITH THE COÖPERATION OF

LESLIE JOHN COMRIE
SOLOMON ACHILLOVICH JOFFE

I

NOS. 1-12

1943-1945

Published by

THE NATIONAL RESEARCH COUNCIL

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Published quarterly in January, April, July and October by the National Research Council, Prince and Lemon Sts., Lancaster, Pa., and Washington, D. C.

All contributions intended for publication in *Mathematical Tables and Other Aids to Computation*, and all Books for review, should be addressed to Professor R. C. ARCHIBALD, Brown University, Providence, R. I.

Entered as second-class matter July 29, 1943, at the post office at Lancaster, Pennsylvania, under the Act of August 24, 1912.

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CONTENTS

I NUMBER 1 JANUARY 1943

Introductory	1
Recent Mathematical Tables (RMT).....	3
Summary index to reviewed tables 1-74.	
Reviews of tables by 75. Benson; 76. Ives; 77. Coast and G. Survey; 78. Peters; 79. Peters; 80. Monroe Calculating Machine Co.; 81. New York Math. Tables Project; 82. Barlow-Comrie; 83. Gushee; 84. Molina; 85. Jaeger; 86. Uhler; 87. Page; 88. Stutz.	
Mathematical Tables—Errata (MTE).....	24
1. Gifford; 2. Briggs; 3. Cunningham and Euler; 4. Comrie.	
Unpublished Mathematical Tables (UMT).....	26
1. Wrench and Cunningham	
Mechanical Aids to Computation (MAC).....	27
1. Seventeenth Century Calculating Machines	
Notes (N).....	29
1. J. R. Airey and E. W. Brown; 2. E. L. Ince; 3. N. Y. Math. Tables Project.	
Queries (Q).....	30
1. Tables to many places of decimals	
Queries—Replies (QR).....	30
1. Tables to many places of decimals	

CONTENTS

I NUMBER 2 APRIL 1943

Tables of Trigonometric Functions in Non-Sexagesimal Arguments.	33-44
Recent Mathematical Tables (RMT)	
Reviews of tables by 89. N. Y. Tables Project; 90. N. Y. Tables Project; 91. Sheppard, and N. Y. Tables Project; 92. Lowan, Davids, etc.; 93. Lowan, etc., and Bickley and Miller; 94. Uhler; 95. Uhler; 96. Uhler; 97. Uhler.....	45-56
Mathematical Tables—Errata (MTE).....	56-59
5. C. G. S. Table; 6. Lowan, etc.; 7. Peters.	
Unpublished Mathematical Tables (UMT).....	59-61
2. Airey; 3. Comrie.	
Mechanical Aids to Computation (MAC).....	61-64
2. Lilley; 3. Comrie; 4. Shannon, and Massey, etc.	
Notes (N).....	64-66
4. Gifford and C. G. S. Tables; 5. C. G. S. vs. Peters; 6. Eight-figure Table of Peters and Comrie; 7. Smithsonian Tables.	

CONTENTS—APRIL (continued)

Queries (Q).....	66-67
2. Scarce Mathematical Tables.	
Queries—Replies (QR).....	67-68
2. Tables to many places of decimals.	
Corrigenda.....	68

CONTENTS

I NUMBER 3 JULY 1943

Mathematical Tables in Reports of the B. A. A. S.....	69-75
Recent Mathematical Tables (RMT)	
Reviews of Tables by, 98. N. Y. Tables Project; 99. Thompson; 100. Comrie and Hartley; 101. Thompson; 102. Merrington and Thompson; 103. Dreisonstock; 104. Ageton; 105. Hydrographic Office; 106. Royal Air Force; 107. C. G. Survey.....	75-85
Mathematical Tables—Errata (MTE)	
8. France, Service Géographique; 9. Various authors; 10. Hudson and Mills; 11. Dreisonstock; 12. Buckingham.....	85-92
Unpublished Mathematical Tables (UMT)	
4. N. Y. Tables Project; 5. N. Y. Tables Project; 6. N. Y. Tables Project; 7. N. Y. Tables Project; 8. Salzer; 9. Escott.....	92-96
Mechanical Aids to Computation (MAC)	
5. Beard.....	96-97
Notes (N)	
8. Henry Briggs and his dates; 9. Cayley and tabulation.....	97-98
Query (Q)	
3. A Shortrede table.....	98
Queries—Replies	
3-4. Tables to many places of decimals; 5. Scarce Mathematical Tables.....	99-100
Corrigenda.....	100

CONTENTS

I NUMBER 4 OCTOBER 1943

Tables occurring in dynamics of structures.....	101-103
Recent Mathematical Tables (RMT)	
Review of tables by 108. Cochran; 109. Swed and Eisenhart; 110. Pearson and Hartley; 111. Merrington; 112. Pearson and Hartley; 113. Jahnke and Emde; 114. Ageton; 115. Comrie; 116. Wittstein; 117. Financial Publ. Co.; 118. Mursi; 119. Sherman and Ewell; 120. Kotani, Amemiya and Simose	103-120

CONTENTS—OCTOBER (continued)

Mathematical Tables—Errata (MTE)
 13. Milne-Thomson; 14. Peters; 15. Parkhurst; 16. N. Y. Tables Project; 17. Tallqvist; 18. Financial Publ. Co.; 19. Bourguet; 20. R. A. Davis 120–124

Unpublished Mathematical Tables (UMT)
 10. Salzer and Hillman; 11. N. Y. Project; 12. N. Y. Project; 13. N. Y. Project; 14. Sarmousakis 125–127

Mechanical Aids to Computation (MAC)
 6. Brown; 7. Brown and Wheeler 127–129

Notes (N)
 10. Briggs and Vieta 129–130

Queries (Q)
 4. Log log tables; 5. Tables of $N^{\frac{1}{2}}$; 6. An Engel table 131

Queries—Replies (QR)
 6. Scarce mathematical tables 132

Corrigenda et Addendum 132

CONTENTS

I NUMBER 5 JANUARY 1944

Note on the Computation of the Bessel Function $I_n(x)$ 133–135

Mathematical Tables in *Phil. Mag.* 135–141

Recent Mathematical Tables (RMT)
 Review of Tables by 121. (War Dept.); 122. (War Dept.); 123. Brown & Sharpe; 124. Nikitin; 125. Peters; 126. Appl. Math. Panel; 127. Hof; 128. Peters; 129. Anderson and Houseman; 130. Kelley; 131. Smith; 132. Smith and Higdon; 133. Lowan and Abramowitz; 134. Lowan, Blanch and Abramowitz; 135. Lowan and Horenstein; 136. Lowan and Salzer; 137. Stratton, Morse, Chu, and Hutner 142–160

Mathematical Tables—Errata (MTE)
 21. Bourget; 22. Comrie; 23. Jahnke and Emde; 24. Kelley; 25. Math. Tables Project; 26. Merrifield; 27. Peters; 28. Brandenburg 160–162

Unpublished Mathematical Tables (UMT)
 15. Joffe; 16. Math. Tables Project; 17. Davis; 18. Math. Tables Project; 19. Math. Tables Project; 20. Math. Tables Project . 163–165

Mechanical Aids to Computation (MAC)
 8. Brown and Wheeler; 9. Brown and Wheeler; 10. Dietzold and Mercner 165–167

CONTENTS—JANUARY (continued)

Notes (N)

11. Alfred Lodge; 12. Interpolation; 13. Johann Theodor Peters;
 14. RMT 98; 15. Russian edition of Barlow's Tables; 16.
 Russian Table of Products..... 167-170

Queries (Q)

7. Briggs' *Arithmetica Logarithmica* 170

Queries—Replies (QR)

7. An Engel Table..... 170-171

- Corrigenda..... 171

CONTENTS

I NUMBER 6 APRIL 1944

- Optimum-Interval Punched-Card Tables..... 173-176

Recent Mathematical Tables (RMT)

- Reviews of Tables by 138 (Math. Tables Project); 139 (Uhler);
 140 (Meissner); 141 (Miller); 142 (Math. T. Project); 143
 (Dwight); 144 (Gupta); 145 (Ko and Wang); 146 (Lehmer);
 147 (Little); 148 (Thompson); 149 (Salzer); 150 (Heuman);
 151 (Math. T. Project); 152 (Powell); 153 (Vandrey); 154
 (Dwight); 155 (Heatley); 156 (Rosenberg); 157 (Lowen and
 Laderman) 176-193

Mathematical Tables—Errata (MTE)

29. Bessel and Hansen; 30. Brown and Hedrick; 31. Chappell;
 32. Dwight; 33. Farr; 34. Greenhill; 35. Hayashi; 36-37.
 Jahnke & Emde; 38-40. Math. T. Project; 41. Thompson;
 42. Weber; 43. Wrinch & Wrinch, Colwell & Hardy 194-200

Unpublished Mathematical Tables (UMT)

21. Math. T. Project; 22. Roots of the Equation $\tan x + ax = 0$; 23. Gupta..... 200-201

Notes (N)

17. Desirable Math. Tables for Republication; 18. Phil. Mag.
 Tables, Suppl. 1; 19. Phil. Mag. Tables, Suppl. 2; 20. Solu-
 tion of the Equation $10 \log x = x$ 201-203

Queries (Q)

8. Roots of the Equation $\tan x = cx$; 9. System of Linear
 Equations..... 203-204

Queries—Replies (QR)

8. Tables of $N^{3/2}$ 204

- Corrigenda..... 204

CONTENTS

I NUMBER 7 JULY 1944

A Guide to

Tables of Bessel Functions

Preface, General Remarks on Notation 206-209

Part I: Guide to Tables and Graphs; Polynomial Approximations and Asymptotic Expansions 210-278

Part II: Bibliography of Authors of Tables and Graphs 279-308

Addenda 308

Corrigenda 308

CONTENTS

I NUMBER 8 OCTOBER 1944

Numerical Testing of Series by Calculations to many Places of Decimals 309-312

Recent Mathematical Tables

Review of Tables by 158 (Uhler); 159 (Vogel); 160 (General Electric Co.); 161 (Todd); 162 (NYMTP); 163 (Salzer); 164 (Fisher & Yates); 165 (Moskovitz); 166 (Takagi); 167 (Bierens de Haan, and Lindman); 168 (Terrill & Sweeny) 312-323

Mathematical Tables—Errata

44. BAASMTc; 45. Brown & Sharpe; 46. Dawson; 47. Fisher & Yates; 48. Hippisley; 49. Jordan; 50. Muskat, Morgan & Meres; 51. NYMTP; 52. NYMTP; 53. Page 323-329

Unpublished Mathematical Tables

24. Salzer; 25. Salzer; [26. Salzer;] 27. Reno; 28. Spenceley 329-331

Mechanical Aids to Computation

11. Adams 331-332

Notes

21. Computing a Table of $\log \Gamma(x)$; 22. Earliest Tables of S and T ; 23. A New Result Concerning a Mersenne Number; 24. Optimum-Interval Punched-Card Tables; 25. A Root of the Equation $10 \log x = x$ 332-335

CONTENTS—OCTOBER (continued)

Queries	
10. Rounding-off Notation	335
Queries—Replies	
9. Log Log Tables; 10. Roots of the Equation $\tan x = cx$; 11. Tables of $N^{3/2}$	336

CONTENTS

I NUMBER 9 JANUARY 1945

Machines for Solving Algebraic Equations	337
Zeros of Certain Bessel Functions of Fractional Order	353
Recent Mathematical Tables	
Review of Tables by 169 (BAASMTC, NYMTP); 170 (Marchant Calculating Machine Co.); 171 (Linnebach); 172 (National Defense Research Committee); 173 (Pucher); 174 (Wright); 175 (Lowan & Salzer); 176 (Salzer); 177 (Stenzel); 178 (Bose); 179 (BAASMTC); 180 (Federal Telephone and Radio Corp.); 181 (NYMTP); 182 (Watson); 183 (Lindemann)	355
Mathematical Tables—Errata	
55 (Bates); 56 (Forsyth); 57 (Karas); 58 (Lommel, Watson); 59 (NYMTP); 60 (Watson)	364
Unpublished Mathematical Tables	
29 (Heppel); 30 (Thomson); 31 (Sang)	367
Mechanical Aids to Computation	
12 (Comrie); 13 (Comrie)	370
Notes	
26. Ageton's Method; 27. Earliest Tables of S and T; 28. Henry Goodwyn, <i>A Tabular Series</i>	370
Queries	
11. Cube Roots; 12. Items in Interpolation History	372
Queries—Replies	
12. Log Log Tables; 13. Tables of $N^{3/2}$	373
Corrigenda et Addenda	375

CONTENTS

I NUMBER 10 APRIL 1945

The Graeffe Process as Applied to Power Series 377

Recent Mathematical Tables

Review of Tables by **184** (Allen); **185** (Emde); **186** (Terrill & Terrill);
187 (Jahnke & Emde); **188** (Chappell & Rohr & Bremiker); **189**
 (Brandenburg); **190** (Alaoglu & Erdős); **191** (Bell); **192** (Jones, ,
193 (National Defense Research Committee); **194** (Serebriiskii) . . 384

Mathematical Tables—Errata

61 (Jahnke & Emde) 391

Unpublished Mathematical Tables

32 (Durfee); **33** (U. S. Dept. of Commerce, Weather Bureau) 399

Mechanical Aids to Computation

14 (King, and Thomas & King) 399

Notes

29. Early Decimal Division of the Sexagesimal Degree; **30.** First
 Published Compound Interest Tables; **31.** First Published Mor-
 tality Table; **32.** Guide (*MTAC* no. 7), Suppl. 1; **33.** New Result
 Concerning a Mersenne Number; **34.** Originators of the Term
 Radian; **35.** *Phil. Mag.* Tables, Suppl. 3; **36.** Zeros of the Bessel
 Functions $J_\nu(x)$ 400

Queries

13. Tables of Integrals 407

Queries—Replies

14. Table of $N^{3/2}$ 407

Corrigenda 408

CONTENTS

I NUMBER 11 JULY 1945

The Tabulation of Mathieu Functions 409

Recent Mathematical Tables

Reviews of Tables by **195** (Beckerley); **196** (Kaván and BAASMTC);
197 (Hydrographic Office); **198** (Hull & Hull); **199** (Wright); **200**
 (Stäblein & Schläfer); **201** (Baldwin); **202** (Bisshopp); **203** (Bloch);
204 (Buchholz); **205** (Buchholz); **206** (Cossar & Erdélyi); **207**
 (NYMTP); **208** (NYMTP); **209** (Schwarz); **210** (Stenzel) 419

CONTENTS—JULY (continued)

Mathematical Tables—Errata	
62 (Burgess); 63 (Kraitichik); 64 (Lommel); 65 (NYMTP); 66 (Page)	427
Unpublished Mathematical Tables	
34 (NYMTP).....	430
Mechanical Aids to Computation	
15 (Kuehni & Peterson).....	430
Notes	
37 . Notation $yer_n x$, $yei_n x$; 38 . A Root of $y = e^y$; 39 . Roots of $\tan x = xf(x)$	431
Queries	
14 . Tables of $\tan^{-1}(m/n)$	431
Queries—Replies	
15 . Cube Roots; 16 . Rounding-off Notation.....	432
Corrigenda et Addendum.....	432

CONTENTS

I NUMBER 12 OCTOBER 1945

Mathematical Tables on Punched Cards.....	433
Recent Mathematical Tables	
Reviews of Tables by 211 (Vriesendorp); 212 (Buerger & Klein); 213 (Beskin); 214 (Holtappel); 215 (NYMTP); 216 (National Defense Research Comm.); 217 (Chebyshev); 218 (Nogrady); 219 (Ryzhik); 220 (Bisshopp); 221 (Karsmenkov); 222 (Corrington & Miehle); 223 (Carsten & McKerrow); 224 (Fränz & Vellat); 225 (Truesdell); 226 (Vandrey); 227 (Hogg); 228 (Wells & Spence); 229 (Goudet & Gratzmuller); 230 (Akad. Na ik, S.S.S.R.); 231 (Gr. Britain, <i>Naut. Almanac</i>); 232 (Herrick).....	436
Mathematical Tables—Errata	
67 (Burgess); 68 (Holtappel); 69 (NYMTP).....	448
Unpublished Mathematical Tables	
35 (Porter); 36 (Uhler); 37 (Westinghouse Electric Corp.); 38 (Wrench).....	451

CONTENTS—OCTOBER (continued)

Mechanical Aids to Computation

16 (Maginniss) 452

Notes

40 Correct but—!; 41 Early Decimal Division of the Sexagesimal Degree; 42 First Mortality Table; 43 Francis William Newman (1805–1897); 44 Table of $\frac{1}{2}Wx/V$ 454

Queries

15 Integral and Functional Tables 459

Queries—Replies

17 Roots of the Equation $\tan x = cx$; 18 Table of $\tan^{-1}(m/n)$ 459

Corrigenda et Addenda 460

Index, *MTAC*, nos. 1–12 461

LANCASTER PRESS, INC., LANCASTER, PA.

CLASSIFICATION OF TABLES

- A. Arithmetical Tables, Mathematical Constants
- B. Powers
- C. Logarithms
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- G. Higher Algebra
- H. Numerical Solution of Equations
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- L. Higher Mathematical Functions
- M. Integrals
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- U. Navigation
- V. Aerodynamics, Hydrodynamics, Ballistics
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