

97. S. LUBKIN & J. J. STOKER, "Stability of columns and strings under periodically varying forces," *Quart. Appl. Math.*, v. 1, 1943, p. 232-235. See *MTAC*, v. 1, p. 415.

The authors list 48 errors in the tables of this article in *Quart. Appl. Math.*, v. 4, Oct. 1946, p. 309-310.

98. F. ZICKERMANN, "Ueber Arbeitsmessung bei Wechselstrom mit besonderer Berücksichtigung des Drehstromarbeitsdynamometers von Siemens & Halske," *Elektrot. Z.*, v. 12, 1891; on p. 511 is a table of  $f(x, y) = \tan y \cdot \tan(x - y)$ .

This table is for  $f(x, y) \leq 1$ ,  $y = 0(1^\circ)45^\circ$ ,  $x - y = [0(5^\circ)90^\circ; 3D]$ . By differencing the following errata were readily found:  $y = 9^\circ$ ,  $x - y = 75^\circ$ , for 0,581, read 0,591;  $y = 20^\circ$ ,  $x - y = 65^\circ$ , for 0,770, read 0,781.

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### UNPUBLISHED MATHEMATICAL TABLES

For other unpublished tabular numbers see RMT 346, 348; MTE 95.

- 52[K].—STUART R. BRINKLEY, JR. & RUTH F. BRINKLEY, *Table of the probability of hitting a circular target*. Ms. prepared by, and in the possession of the authors, R. D. 3, Coraopolis, Pennsylvania.

It is readily verified that the probability that the point of impact of a missile aimed at the origin of a rectangular system of coordinates will lie within a circle of radius  $r$  whose center is at a distance  $R$  from the origin is

$$p(r, R) = e^{-R^2} \int_0^{r^2} e^{-t} I_0(2Rt) dt,$$

if the probability distributions for the pair of rectangular coordinates are Gaussian;  $I_0$  being the modified Bessel function of the first kind, zeroth order. A table has been prepared of the function  $p(r, R)$ , for  $r = 0(.1)5$ ;  $R = [0(.1)5; 5S]$ . The construction of the table was made possible by a grant from the George Sheffield Fund of Yale University.

We undertook the construction of the table because of applications of the related functions

$$P(x, y) = e^{x+y} p(\sqrt{x}, \sqrt{y}),$$

which is the solution of

$$\frac{\partial^2 P}{\partial x \partial y} = P, \quad P(0, y) = 0, \quad P(x, 0) = e^x - 1.$$

It appears to have numerous and rather diverse applications. It occurs, for example, in the theory of ion-exchange water softening columns (H. C. THOMAS, *Amer. Chem. Soc., Jn.*, v. 66, 1944, p. 1664f), the theory of heat exchange between a fluid and a porous solid (A. ANZELIUS, *Z. angew. Math. Mech.*, v. 6, 1926, p. 291f, and T. E. W. SCHUMANN, *Franklin Inst., Jn.*, v. 208, 1929, p. 405f), and in the extension of the latter theory to the case where the solid is generating heat, as in a catalytic chemical reaction (S. R. BRINKLEY, unpublished paper, in the press). However, the function  $P$  is considerably less well suited to tabulation than is the function  $p$ .

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