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A. Arithmetical Tables. Mathematical Constants

B. Powers

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D. Circular Functions

E. Hyperbolic and Exponential Functions

F. Theory of Numbers

G. Higher Algebra

H. Numerical Solution of Equations

I. Finite Differences. Interpolation

J. Summation of Series

K. Statistics

L. Higher Mathematical Functions

M. Integrals

N. Interest and Investment

O. Actuarial Science

P. Engineering

Q. Astronomy

R. Geodesy

S. Physics, Geophysics, Crystallography

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U. Navigation

V. Aerodynamics, Hydrodynamics, Ballistics

W. Economics and Social Sciences

X Numerical Analysis and Applied Mathematics

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