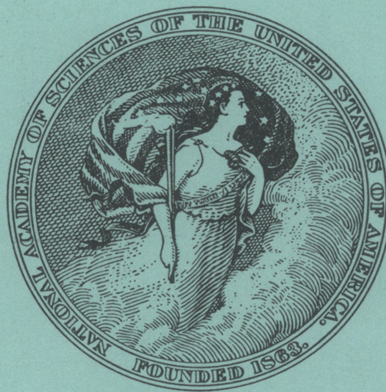


July 1962 · Vol. 16, No. 79

Mathematics of Computation

A journal devoted to advances in numerical analysis,
the application of computational methods, mathematical tables,
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Formerly: *Mathematical Tables and other Aids to Computation*

Published Quarterly for the
National Academy of Sciences—National Research Council
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National Academy of Sciences—National Research Council
Washington, D. C.

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Published Quarterly for the
NATIONAL ACADEMY OF SCIENCES—NATIONAL RESEARCH COUNCIL
By the

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Providence, Rhode Island

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