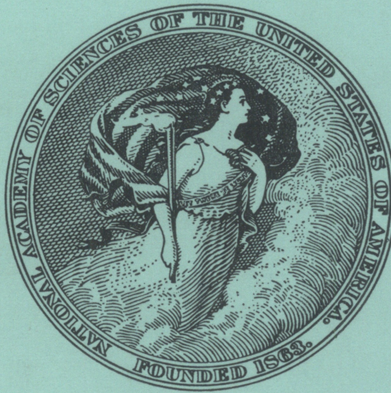


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the application of computational methods, mathematical tables,
high-speed calculators and other aids to computation



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Mathematics of Computation

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