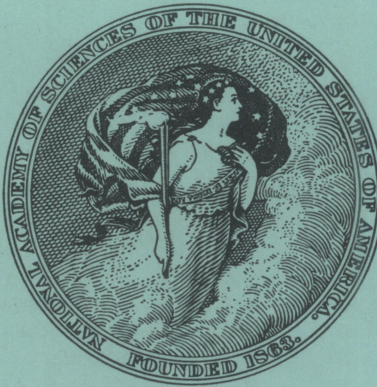


April 1964 • Vol. 18, No. 86

Mathematics of Computation

A journal devoted to advances in numerical analysis,
the application of computational methods, mathematical tables,
high-speed calculators and other aids to computation



Published Quarterly for the
National Academy of Sciences—National Research Council
By the
American Mathematical Society

Editorial Committee
Division of Mathematics
National Academy of Sciences—National Research Council
Washington, D. C.

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Subscriptions, address changes, business communications and payments should be sent to:

AMERICAN MATHEMATICAL SOCIETY
190 Hope Street
Providence, Rhode Island 02906

Published Quarterly for the

NATIONAL ACADEMY OF SCIENCES—NATIONAL RESEARCH COUNCIL
by the

AMERICAN MATHEMATICAL SOCIETY
Providence, Rhode Island

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Printed in the United States of America

Second-class postage paid at Providence, Rhode Island and at additional mailing offices.

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