## Mathematics of <br> Computation

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## reviews in

## edited by william J. Leveque

In these six volumes Professor LeVeque has attempted to include all the reviews in Volumes 1 - 44 of Mathematical Reviews which bear directly on questions commonly regarded as part of number theory. The 14,426 reviews reprinted here include all but a handful of those that appeared in the section of MR entitled Theory of Numbers (those not included seem to have been misclassified originally), together with about three thousand items selected from other sections. These supplementary selections were made partly by scanning relevant sections of MR, and partly by checking all articles cited in reviews already included.
A difficulty lay in deciding what is and what is not number theory. Wherever one stops there is a gray area just beyond, and in the end personal judgments must enter. The editor intended to be rather liberal on inclusion questions, and approximately equally so in the various fringe areas, but could give no short set of criteria which would account for all the decisions made.
Some of the work's useful features: The editor retained the original MR reference for each review (e.g., " $10,588 \mathrm{C}$ " means the third review on p. 588 of vol. 10), and added an "appearance number" specifying the location in the present volumes by chapter, section and number within the section. Articles cited in reviews are frequently referenced by $M R$ numbers, and the equivalent appearance numbers are indicated by equations following the review, when the cited article occurs in these volumes.
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