# Mathematics of Computation

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Manuscripts should be typewritten double-spaced in the format used by the journal. For journal abbreviations, see the latest *Mathematical Reviews* volume index. An author should submit the original and one copy of the manuscript and retain one copy. The author may suggest an appropriate editor for his paper. It is recommended that the author acquaint himself with the pertinent material contained in "A Manual for Authors of Mathematical Papers," which is available from the American Mathematical Society. All contributions intended for publication and all books for review should be addressed to James H. Bramble, Chairman, Editorial Committee, Mathematics of Computation, Center for Applied Mathematics, 275 Olin Hall, Cornell University, Ithaca, New York 14853. Institutions sponsoring research reported in the journal are assessed page and microfiche charges.

Each article submitted for publication must be accompanied by a brief and reasonably self-contained abstract, and by AMS (MOS) subject classification numbers. If a list of key words and phrases is included, it will be printed as a footnote on the first page. A list of the classification numbers may be found in the Index to Mathematical Reviews, Volume 39 (June 1970).

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# NONLINEAR PROGRAMMING

# Edited by

# Richard W. Cottle and Carlton E. Lemke

Harold W. Kuhn, Nonlinear programming: A historical view

Garth P. McCormick, Optimality criteria in nonlinear programming

David G. Luenberger, Algorithmic analysis in constrained optimization

- M. J. D. Powell, Some global convergence properties of a variable metric algorithm for minimization without exact line searches
- B. Curtis Eaves, A short course in solving equations with PL homotopies
- R. Tyrrell Rockafellar, Lagrange multipliers in optimization
- O. L. Mangasarian, Unconstrained methods in nonlinear programming
- J. E. Dennis, Jr., A brief survey of convergence results for quasi-Newton methods.

These Proceedings are based on lectures delivered at the symposium on Nonlinear Programming held March 23 and 24, 1975, as part of the American Mathematical Society's annual New York meeting. This event was the ninth in a series of Symposia in Applied Mathematics jointly sponsored by the Society for Industrial and Applied Mathematics and the American Mathematical Society with financial support from the Energy Research and Development Agency (formerly the Atomic Energy Commission) and the National Science Foundation.

The organizing committee for the symposium consisted of R.W. Cottle (chairman), C.E. Lemke, S.M. Robinson, and J.B. Rosen. The committee's intent was to help bring to the attention of a larger mathematical audience some of the history, theory, applications and vigorous research activity of the Nonlinear Programming field. The editors feel that the results included in these Proceedings can be recommended as well to the worker in the field as to the interested initiate.

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