# Mathematics of <br> <br> Computation 

 <br> <br> Computation}

Coden MCMPAF<br>Volume 31, Number 138

Pages 333-617
April 1977

Published by the American Mathematical Society<br>Providence, Rhode Island

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## Corrigendum

## Bellman \& Wing <br> Microfiche Supplement

Addendum to "The Orders of the Known Simple Groups as Far as One Trillion" Craig Cato

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# NONLINEAR PROGRAMMING 

## Edited by

Richard W. Cottle and Carlton E. Lemke
Harold W. Kuhn, Nonlinear programming: A historical view
Garth P. McCormick, Optimality criteria in nonlinear programming
David G. Luenberger, Algorithmic analysis in constrained optimization
M. J. D. Powell, Some global convergence properties of a variable metric algorithm for minimization without exact line searches
B. Curtis Eaves, $A$ short course in solving equations with PL homotopies
R. Tyrrell Rockafellar, Lagrange multipliers in optimization
O. L. Mangasarian, Unconstrained methods in nonlinear programming
J. E. Dennis, Jr., A brief survey of convergence results for quasi-Newton methods .

These Proceedings are based on lectures delivered at the symposium on Nonlinear Programming held March 23 and 24, 1975, as part of the American Mathematical Society's annual New York meeting. This event was the ninth in a series of Symposia in Applied Mathematics jointly sponsored by the Society for Industrial and Applied Mathematics and the American Mathematical Society with financial support from the Energy Research and Development Agency (formerly the Atomic Energy Commission) and the National Science Foundation.

The organizing committee for the symposium consisted of R.W. Cottle (chairman), C.E. Lemke, S. M. Robinson, and J. B. Rosen. The committee's intent was to help bring to the attention of a larger mathematical audience some of the history, theory, applications and vigorous research activity of the Nonlinear Programming field. The editors feel that the results included in these Proceedings can be recommended as well to the worker in the field as to the interested initiate.

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