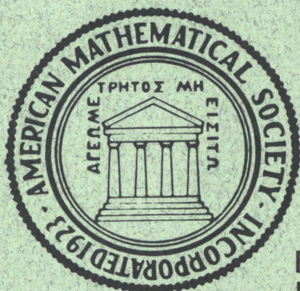


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April 1979

Volume 33, Number 146, Pages 435–848

**Published by the American Mathematical Society
Providence, Rhode Island USA**

ISSN 0025-5718

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SUBSCRIPTION INFORMATION: MATHEMATICS OF COMPUTATION is published quarterly in one volume per year, with issues numbered serially since Volume 1, Number 1. Subscription prices for Volume 33 (1979) are \$55.00 list; \$39.00 institutional member; \$20.00 individual member; \$29.00 member of CBMS organizations. Combination paper and microform (microfiche or microfilm) subscription prices are \$74.00 list; \$52.00 institutional member. Microfiche of each issue will be mailed the fastest way before the camera copy is sent to the printer.

BACK NUMBER INFORMATION: Back number prices *per volume* are for Volumes 1–27, \$36.00 list, \$27.00 member; for Volumes 28–29, \$54.00 list, \$40.50 member; for Volume 30, \$72.00 list, \$54.00 member; for Volumes 31–32, \$84.00 list, \$63.00 member. Back volumes are also available on 16mm positive or negative microfilm. The microfilm may be mounted on spools or in Kodak or 3M cartridges. Only current subscribers are eligible to purchase back volumes on microfilm. Write to the AMS for a detailed price list.

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Second class postage paid at Providence, Rhode Island, and additional mailing offices.

U.S. Postal Service Publication No. 333980

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