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April 1986

Volume 46, Number 174, Pages 361–776

**Published by the American Mathematical Society  
Providence, Rhode Island USA**

ISSN 0025-5718



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MATHEMATICS OF COMPUTATION is published quarterly by the American Mathematical Society, 201 Charles Street, Providence, RI 02904. Second-class postage is paid at Providence, Rhode Island, and additional mailing offices. Postmaster: Send address changes to Mathematics of Computation, American Mathematical Society, P.O. Box 6248, Providence, RI 02940.

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Printed in the United States of America

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# MATHEMATICS OF COMPUTATION

## TABLE OF CONTENTS

April 1986

<b>J. H. Bramble, J. E. Pasciak and A. H. Schatz</b> , An Iterative Method for Elliptic Problems on Regions Partitioned into Substructures.....	361
<b>M. E. Cayco and R. A. Nicolaides</b> , Finite Element Technique for Optimal Pressure Recovery from Stream Function Formulation of Viscous Flows .....	371
<b>Ami Harten</b> , On a Large Time-Step High Resolution Scheme.....	379
<b>J. Thomas Beale</b> , A Convergent 3-D Vortex Method With Grid-Free Stretching.....	401
<b>Laurence Halpern</b> , Artificial Boundary Conditions for the Linear Advection Diffusion Equation.....	425
<b>S. McCormick and J. Thomas</b> , The Fast Adaptive Composite Grid (FAC) Method for Elliptic Equations.....	439
<b>Arthur G. Werschulz</b> , Complexity of Indefinite Elliptic Problems .....	457
<b>Christian Schmeiser</b> , Approximate Solution of Boundary Value Problems on Infinite Intervals by Collocation Methods .....	479
<b>Per Lötstedt and Linda Petzold</b> , Numerical Solution of Nonlinear Differential Equations with Algebraic Constraints I: Convergence Results for Backward Differentiation Formulas.....	491
<b>Takuya Tsuchiya</b> , On Two Methods for Approximating Minimal Surfaces in Parametric Form .....	517
<b>Ted Speevak</b> , An Efficient Algorithm for Obtaining the Volume of a Special Kind of Pyramid and Application to Convex Polyhedra .....	531
<b>Nicholas J. Higham</b> , Newton's Method for the Matrix Square Root .....	537
<b>Gradimir V. Milovanović and Staffan Wrigge</b> , Least Squares Approximation With Constraints.....	551
<b>Holger Mettke</b> , Convex Interpolation by Splines of Arbitrary Degree.....	567
<b>Reinhard Farwig</b> , Rate of Convergence of Shepard's Global Interpolation Formula.....	577
<b>Klaus-Jürgen Förster and Georg-Peter Ostermeyer</b> , On Weighted Chebyshev-Type Quadrature Formulas.....	591
<b>Helmut F. Bauer</b> , Tables of the Roots of the Associated Legendre Function with Respect to the Degree.....	601
<b>D. P. McCarthy</b> , Effect of Improved Multiplication Efficiency on Exponentiation Algorithms Derived from Addition Chains .....	603
<b>Hiroyoshi Yamaki</b> , A Conjecture of Frobenius and the Sporadic Simple Groups, II.....	609
<b>David Easton</b> , Effective Irrationality Measures for Certain Algebraic Numbers.....	613
<b>Nicholas Tzanakis</b> , A Remark on a Theorem of W. E. H. Berwick .....	623
<b>Thomas J. Kretschmer</b> , Construction of Elliptic Curves with Large Rank ...	627
<b>Markus A. Reichert</b> , Explicit Determination of Nontrivial Torsion Structures of Elliptic Curves Over Quadratic Number Fields.....	637
<b>Günter Lettl</b> , A Lower Bound for the Class Number of Certain Cubic Number Fields .....	659
<b>J. van de Lune, H. J. J. te Riele and D. T. Winter</b> , On the Zeros of the Riemann Zeta Function in the Critical Strip. IV.....	667



<b>D. H. Lehmer, K. Mahler and A. J. van der Poorten</b> , Integers with Digits 0 or 1.....	683
<b>G. C. Kurtz, Daniel Shanks and H. C. Williams</b> , Fast Primality Tests for Numbers Less Than $50 \cdot 10^9$ .....	691
<b>Ray P. Steiner</b> , On Mordell's Equation $y^2 - k = x^3$ : A Problem of Stolarsky	703
<b>Mok-Kong Shen</b> , On the Congruence $2^{n-k} \equiv 1 \pmod{n}$ .....	715
<b>D. R. Stinson and E. Seah</b> , 284457 Steiner Triple Systems of Order 19 Contain a Subsystem of Order 9.....	717
<b>Richard Blecksmith, John Brillhart and Irving Gerst</b> , A Computer-Assisted Investigation of Ramanujan Pairs.....	731
<b>J. Lagrange and J. Leech</b> , Two Triads of Squares .....	751
<b>Reviews and Descriptions of Tables and Books</b> .....	759
Hyman 4, Davis and Rabinowitz 5, Bleistein 6, Nonweiler 7, Anderson, Tannehill and Pletcher 8, Crank 9, Parter, Editor 10, Singh, Burry and Watson, Editors 11, Griffiths, Editor 12, Fitch, Editor 13, Birkhoff and Schoenstadt, Editors 14, Graves-Morris, Saff and Varga, Editors 15, Boerner et al., Editors 16, Fischer and Smith, Editors 17, Turner, Editor 18	
<b>Corrigenda</b> .....	771
Heald, Brent, van de Lune, te Riele and Winter, van de Lune and te Riele	
<b>Author Index</b> .....	773
<b>Supplement to "A Convergent 3-D Vortex Method With Grid-Free Stretching"</b> by <b>J. Thomas Beale</b> .....	S15
<b>Supplement to "On Weighted Chebyshev-Type Quadrature Formulas"</b> by <b>Klaus-Jürgen Förster and Georg-Peter Ostermeyer</b> .....	S21
<b>Supplement to "Table of the Roots of the Associated Legendre Function with Respect to the Degree"</b> by <b>Helmut F. Bauer</b> .....	S29
<b>Supplement to "A Conjecture of Frobenius and the Sporadic Simple Groups. II"</b> by <b>Hiroyoshi Yamaki</b> .....	S43
<b>Microfiche Supplement</b>	
<b>Markus A. Reichert</b> , Explicit Determination of Nontrivial Torsion Structures of Elliptic Curves Over Quadratic Number Fields	

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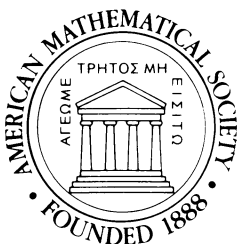
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Compiled and Edited by Lance W. Small

Department of Mathematics, University of California, San Diego

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Each review has an "appearance number" specifying the location of the review by chapter, section and number within the section. By and large, reviews within one section are arranged in "rough" chronological order (i.e., by appearance in Mathematical Reviews). The principal exceptions are papers in a series and very closely related papers. If a cited review occurs in these volumes, then its appearance number is listed after the review in which it is cited.

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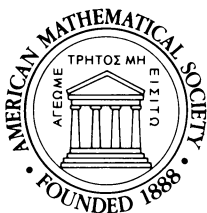
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### Contents

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<b>D. H. Lehmer, K. Mahler and A. J. van der Poorten</b> , Integers with Digits 0 or 1 .....	683
<b>G. C. Kurtz, Daniel Shanks and H. C. Williams</b> , Fast Primality Tests for Numbers Less Than $50 \cdot 10^9$ .....	691
<b>Ray P. Steiner</b> , On Mordell's Equation $y^2 - k = x^3$ : A Problem of Stolarsky .....	703
<b>Mok-Kong Shen</b> , On the Congruence $2^{n-k} \equiv 1 \pmod{n}$ .....	715
<b>D. R. Stinson and E. Seah</b> , 284457 Steiner Triple Systems of Order 19 Contain a Subsystem of Order 9 .....	717
<b>Richard Blecksmith, John Brillhart and Irving Gerst</b> , A Computer-Assisted Investigation of Ramanujan Pairs .....	731
<b>J. Lagrange and J. Leech</b> , Two Triads of Squares .....	751
<b>Reviews and Descriptions of Tables and Books</b> .....	759
Hyman 4, Davis and Rabinowitz 5, Bleistein 6, Nonweiler 7, Anderson, Tannehill and Pletcher 8, Crank 9, Parter, Editor 10, Singh, Burry and Watson, Editors 11, Griffiths, Editor 12, Fitsch, Editor 13, Birkhoff and Schoenstadt, Editors 14, Graves-Morris, Saff and Varga, Editors 15, Boerner et al., Editors 16, Fischer and Smith, Editors 17, Turner, Editor 18	
<b>Corrigenda</b> .....	771
Heald, Brent, van de Lune, te Riele and Winter, van de Lune and te Riele	
<b>Author Index</b> .....	773
<b>Supplement to "A Convergent 3-D Vortex Method With Grid-Free Stretching"</b> by <b>J. Thomas Beale</b> .....	S15
<b>Supplement to "On Weighted Chebyshev-Type Quadrature Formulas"</b> by <b>Klaus-Jürgen Förster and Georg-Peter Ostermeyer</b> .....	S21
<b>Supplement to "Table of the Roots of the Associated Legendre Function with Respect to the Degree"</b> by <b>Helmut F. Bauer</b> .....	S29
<b>Supplement to "A Conjecture of Frobenius and the Sporadic Simple Groups. II"</b> by <b>Hiroyoshi Yamaki</b> .....	S43
<b>Microfiche Supplement</b>	
<b>Markus A. Reichert</b> , Explicit Determination of Nontrivial Torsion Structures of Elliptic Curves Over Quadratic Number Fields	



# MATHEMATICS OF COMPUTATION

## TABLE OF CONTENTS

April 1986

<b>J. H. Bramble, J. E. Pasciak and A. H. Schatz</b> , An Iterative Method for Elliptic Problems on Regions Partitioned into Substructures.....	361
<b>M. E. Cayco and R. A. Nicolaides</b> , Finite Element Technique for Optimal Pressure Recovery from Stream Function Formulation of Viscous Flows .....	371
<b>Ami Harten</b> , On a Large Time-Step High Resolution Scheme.....	379
<b>J. Thomas Beale</b> , A Convergent 3-D Vortex Method With Grid-Free Stretching.....	401
<b>Laurence Halpern</b> , Artificial Boundary Conditions for the Linear Advection Diffusion Equation.....	425
<b>S. McCormick and J. Thomas</b> , The Fast Adaptive Composite Grid (FAC) Method for Elliptic Equations.....	439
<b>Arthur G. Werschulz</b> , Complexity of Indefinite Elliptic Problems .....	457
<b>Christian Schmeiser</b> , Approximate Solution of Boundary Value Problems on Infinite Intervals by Collocation Methods .....	479
<b>Per Lötstedt and Linda Petzold</b> , Numerical Solution of Nonlinear Differential Equations with Algebraic Constraints I: Convergence Results for Backward Differentiation Formulas.....	491
<b>Takuya Tsuchiya</b> , On Two Methods for Approximating Minimal Surfaces in Parametric Form .....	517
<b>Ted Speevak</b> , An Efficient Algorithm for Obtaining the Volume of a Special Kind of Pyramid and Application to Convex Polyhedra .....	531
<b>Nicholas J. Higham</b> , Newton's Method for the Matrix Square Root .....	537
<b>Gradimir V. Milovanović and Staffan Wrigge</b> , Least Squares Approximation With Constraints.....	551
<b>Holger Mettke</b> , Convex Interpolation by Splines of Arbitrary Degree.....	567
<b>Reinhard Farwig</b> , Rate of Convergence of Shepard's Global Interpolation Formula.....	577
<b>Klaus-Jürgen Förster and Georg-Peter Ostermeyer</b> , On Weighted Chebyshev-Type Quadrature Formulas.....	591
<b>Helmut F. Bauer</b> , Tables of the Roots of the Associated Legendre Function with Respect to the Degree.....	601
<b>D. P. McCarthy</b> , Effect of Improved Multiplication Efficiency on Exponentiation Algorithms Derived from Addition Chains .....	603
<b>Hiroyoshi Yamaki</b> , A Conjecture of Frobenius and the Sporadic Simple Groups, II.....	609
<b>David Easton</b> , Effective Irrationality Measures for Certain Algebraic Numbers.....	613
<b>Nicholas Tzanakis</b> , A Remark on a Theorem of W. E. H. Berwick .....	623
<b>Thomas J. Kretschmer</b> , Construction of Elliptic Curves with Large Rank ...	627
<b>Markus A. Reichert</b> , Explicit Determination of Nontrivial Torsion Structures of Elliptic Curves Over Quadratic Number Fields.....	637
<b>Günter Lettl</b> , A Lower Bound for the Class Number of Certain Cubic Number Fields .....	659
<b>J. van de Lune, H. J. J. te Riele and D. T. Winter</b> , On the Zeros of the Riemann Zeta Function in the Critical Strip. IV.....	667

(Continued on inside back cover)