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PROVIDENCE, RHODE ISLAND USA

ISSN 0025-5718

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This publication was typeset using AMS-TEX, the American Mathematical Society's TEX macro system.

10 9 8 7 6 5 4 3 2 1 98 97 96 95 94 93

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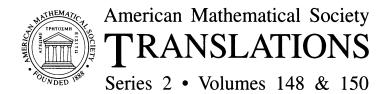
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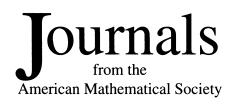
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