

5005-C1-50

**Jared Tanner\***, University of Utah and, University of Edinburgh. *Phase transitions for the recovery of  $k$ -sparse signals using linear programming: finite dimensional bounds.*

Consider an underdetermined system of linear equations  $y = Ax$  with known  $y$  and  $n \times N$ , matrix  $A$  with  $n < N$  for  $\delta \in (0, 1)$ . We seek the sparsest solution, i.e., the  $x$  with fewest nonzeros satisfying  $y = Ax$ . In general this problem is NP-hard; however, for many matrices  $A$  there is a threshold phenomenon: if the sparsest solution is sufficiently sparse, it can be found by linear programming. Quantitative values for a strong and weak threshold will be presented. The strong threshold guarantees the recovery of the sparsest solution  $x_o$ , whereas a weaker sparsity constraint ensures the recovery of the sparsest solution for most  $x_o$ . Thresholds will be presented both in the asymptotic limit as  $N \rightarrow \infty$  as well as for finite values of  $N$ . This work was joint with David L. Donoho. (Received July 03, 2007)