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**Alexandr N. Grishkov\*** (shuragri@gmail.com), , Brazil. *An analogue of Campbell-Hausdorff formula in characteristic  $p > 0$ .* Preliminary report.

Let  $A = A_k(x, y)$  be a free algebra in some variety  $\mathcal{V}$  of associative algebras with free generators  $x, y$ , over a ring  $k$ . Then  $A = \sum_{i=0}^{\infty} \oplus A_i$ , where  $A_i$  is a subspace of  $A$  of homogenous elements of degree  $i$ .

By  $\mathcal{A}$  we denote the  $k$ -algebra of series  $f = \sum_{i=0}^{\infty} f_i$ ,  $f_i = f_i(x, y) \in A_i$ .

By definition  $A_f$  is the minimal  $k$ -submodule of  $A$  such that  $x, y \in A_f$  and for any  $v, w \in A_f$  and any  $f_i$  we have that  $f_i(v, w) \in A_f$ .

Let  $g(x) = 1 + x + g_2x^2 + \dots \in k[[x]] \subset \mathcal{A}$ . Then there exists  $l(x) \in k[[x]]$  such that  $l(g(x)) = g(l(x)) = x$ . Define Campbell-Hausdorff  $g$ -serie  $CH(g) \in \mathcal{A}$  such that

$$CH(g)(x, y) = l(g(x)g(y)).$$

A serie  $e(x) = 1 + x + \dots \in k[[x]]$ , is an  $\mathcal{V}_k$ -exponent if for any other  $g(x) = 1 + x + \dots \in k[[x]]$  we have that from  $A_{CH(g)} \subseteq A_{CH(e)}$  hence  $A_{CH(g)} = A_{CH(e)}$ .

The main result is:

Let  $\mathcal{V}$  be any variety of associative algebras over the ring of  $p$ -adic intergers  $\mathbf{Z}_p$ . Let  $e(x) = 1 + x + \dots, \Phi(x) = x + \dots \in \mathbf{Z}_p[[x]]$  be such that

$$e'(x) = \Phi(x^{p-1})e(x),$$

then  $e(x)$  is  $\mathcal{V}_{\mathbf{Z}_p}$ -exponent. (Received January 30, 2008)