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We discuss some asymptotic properties for solutions of general convection-diffusion equations

$$u_t + \operatorname{div} f(x, t, u) = \operatorname{div}(A(x, t, u)\nabla u), \quad x \in R^n, t > 0,$$

with initial data  $u(x, 0) = u_0(x) \in L^p(R^n)$ ,  $1 \leq p < \infty$ . Under suitable assumptions on  $f$  and  $A$ , we show

$$\|u(\cdot, t)\|_{L^{2p}} \leq C(n, p)\|u_0\|_{L^p}(t\mu(t))^{-\frac{n}{4p}},$$

where  $\mu(t)$  is a positive non-increasing function such that  $\langle A(x, t, \xi)\xi, \xi \rangle \geq \mu(t)|\xi|^2$ ,  $\forall \xi \in R^n$ . Moreover, we discuss how these bounds can be used to obtain an  $L^\infty$  estimate

$$\|u(\cdot, t)\|_\infty \leq K(n, p)\|u_0\|_p(t\mu(t))^{-\frac{n}{2p}}.$$

Some interesting applications of these properties are also mentioned. (Received January 24, 2008)