Meeting: 998, Houston, Texas, SS 21A, Special Session on Homological Algebra of Commutative Rings

998-13-251 Lars Winther Christensen\* (winther@math.ku.dk), Matematisk Afdeling, Universitetsparken 5, DK-2100 Copenhagen O, Denmark, and Srikanth Iyengar. *G-dimension of Almost Finite Modules.* Preliminary report.

The G-dimension for f.g. modules over a commutative, Noetherian, local ring R was introduced by M. Auslander in the late 1960'ies. It is a refinement of the classical projective dimension and obeys the so-called Auslander-Bridger formula:

 $\operatorname{G-dim}_R M = \operatorname{depth}_R - \operatorname{depth}_R M.$ 

This formula has now been extended to almost finite modules: If  $\varphi : R \to S$  is a local homomorphism (i.e. mapping the maximal ideal  $\mathfrak{m}$  of R into that of S), and M is a f.g. S-module with finite G-flat dimension over R, then

$$\mathrm{Gfd}_R M = \mathrm{depth}_R - \mathrm{depth}_R M.$$

Here the G-flat dimension is an extension of the G-dimension to non-finite modules, and depth<sub>R</sub>M is the number of the first non-vanishing  $\text{Ext}_R(R/\mathfrak{m}, M)$  module. The talk will outline the proof of this formula; it draws on a number of recent results in the theory of Gorenstein dimensions. (Received February 29, 2004)