

**Meeting:** 998, Houston, Texas, SS 5A, Special Session on Associative Rings

998-06-60            **Rogelio Fernández-Alonso\*** (rojo99@prodigy.net.mx), Sur 111-A #439, Col. Héroes de Churubusco, 09090 México, D.F., Mexico, and **Silvia Gavito** (silvia\_gavito@yahoo.com), Mexico. *The Lattice of Preradicals over  $\mathbb{Z}_p^n$ .*

In the early 40's Kulikov proved a well-known structure theorem on p-groups. As a consequence, every bounded p-group is a direct sum of cyclic groups; so the  $\mathbb{Z}_p^n$ -modules are just direct sums of ideals of  $\mathbb{Z}_p^n$ . Therefore, any preradical over this ring is determined by its behavior on these ideals, which form a finite chain of length  $n$ . The order lattice of preradicals over  $\mathbb{Z}_p^n$  is isomorphic to the order lattice of certain ascending paths over the plane  $n \times n$ -lattice. We present some of its properties: finite with cardinality  $2^n$ , distributive, self-dual and graded with rank  $\frac{n(n+1)}{2}$ . We also describe the correspondent posets of (co)irreducible and (co)prime elements. (Received January 15, 2004)