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and **Florian Enescu\*** ([enescu@math.utah.edu](mailto:enescu@math.utah.edu)), Department of Mathematics, University of  
Utah, Salt Lake City, UT 84112. *The structure of  $F$ -pure rings.*

For a reduced  $F$ -finite ring  $R$  of characteristic  $p > 0$  and  $q = p^e$  one can write  $R^{1/q} = R^{a_q} \oplus M_q$ , where  $M_q$  has no free direct summands over  $R$ . We investigate the structure of  $F$ -finite,  $F$ -pure rings  $R$  by studying how the numbers  $a_q$  grow with respect to  $q$ . This growth is quantified by the splitting dimension and the splitting ratios of  $R$  which we study in detail. We also prove the existence of a special prime ideal  $P(R)$  of  $R$ , called the splitting prime, that has the property that  $R/P(R)$  is strongly  $F$ -regular. We show that this ideal captures significant information with regard to the  $F$ -purity of  $R$ .

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