

998-53-132

**Pralay Chatterji** ([pralay@math.rice.edu](mailto:pralay@math.rice.edu)), Department of Mathematics, Rice University, Houston, TX 77005-1892, and **Dave Witte Morris\*** ([Dave.Morris@uleth.ca](mailto:Dave.Morris@uleth.ca)), Department of Math and Comp Sci, University of Lethbridge, Lethbridge, Alberta T1K 3M4, Canada. *Geometric interpretation of the  $\mathbb{Q}$ -rank of a locally symmetric space*. Preliminary report.

Let  $X = \Gamma \backslash G / K$  be a locally symmetric space of finite volume (and assume  $G$  is semisimple). The  $\mathbb{Q}$ -rank of  $X$  is defined from algebraic properties of the discrete group  $\Gamma$ , but it has geometric interpretations. In particular, a slight variant of a conjecture of G. Tomanov and B. Weiss states that the  $\mathbb{Q}$ -rank should be equal to the maximum dimension of a closed, simply connected flat in  $X$ . (A *flat* in a Riemannian manifold is a totally geodesic, flat submanifold.) This is analogous to the fact that if  $\tilde{X} = G / K$  is a symmetric space, then the  $\mathbb{R}$ -rank of  $G$  is equal to the maximum dimension of a closed, simply connected flat in  $\tilde{X}$ . We discuss  $\mathbb{Q}$ -rank and progress toward a proof of this conjecture. (Received February 21, 2004)