

Meeting: 1000, Albuquerque, New Mexico, SS 12A, Special Session on Regularity in PDEs and Harmonic Analysis

1000-35-56 **Laura de Carli*** (decarlil@fiu.edu), Florida International University, Department of Mathematics, DM building, Univ. Park, Miami, FL 33199, and **Steve Hudson**. *Unique continuation for second order elliptic operators: a non-Carleman approach*. Preliminary report.

We prove a unique continuation theorem for the differential inequality

$$|\operatorname{div}(\lambda(x)\nabla u)| \leq |V(x)u(x)|, \quad u \in H^{2,1}(\mathbf{R}^n) \quad (1)$$

where $\lambda(x)$ is a Lipschitz continuous matrix which satisfies

$$\langle \lambda(x)v, v \rangle \geq 0, \quad v \in \mathbf{R}^n.$$

Under suitable assumptions on $V(x)$, we prove that every $H^{2,1}$ solution of the differential inequality (1) which vanishes identically outside of a compact set is $\equiv 0$. We also prove a strong unique continuation theorem for nonnegative solutions of the differential inequality

$$|\Delta u(x)| \leq |V(x)u(x)|.$$

which is a special case of (1). Our proofs do not use Carleman type inequalities.

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