

Meeting: 1001, Evanston, Illinois, SS 14A, Special Session on Nonlinear Waves

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Considered here are the quarter-plane problem for the BBM-equation

$$\left. \begin{aligned} u_t + u_x + uu_x - u_{xxt} &= 0, & x \geq 0, & t > 0, \\ u(0, t) &= g(t), & t \geq 0, \\ u(x, 0) &= 0, & x \geq 0 \end{aligned} \right\} \quad (1)$$

and the same equation with two-point boundary values

$$\left. \begin{aligned} v_t + v_x + vv_x - v_{xxt} &= 0, & 0 \leq x \leq L, & t > 0, \\ v(0, t) &= g(t), v(L, t) = 0, & t \geq 0, \\ v(x, 0) &= 0, & 0 \leq x \leq L. \end{aligned} \right\} \quad (2)$$

Suppose the following compatible conditions

$$u(0, 0) = v(0, 0) = g(0) = 0$$

hold true. The main result is that if $g \in H^1(\mathbb{R}^+)$, then both problems are well posed in $C^\infty(\mathbb{R}^+)$ globally in time, and for any fixed point $(x, t) \in \mathbb{R}^+ \times \mathbb{R}^+$, $\lim_{L \rightarrow \infty} v(x, t) = u(x, t)$. (Received August 31, 2004)