

**Meeting:** 1005, Newark, Delaware, SS 9A, Special Session on Arithmetic Groups and Related Topics

1005-22-31            **Gopal Prasad\*** (gprasad@umich.edu), Department of Mathematics, University of Michigan, Ann Arbor, MI 48109-1109. *Zariski-dense subgroups of semisimple Lie groups and Number theory.*

I will report on some recent joint work with Andrei Rapinchuk.

Given a finitely generated subfield  $K$  of  $\mathbb{R}$ , a finitely generated extension field  $L$  of  $K$ , a semisimple algebraic group  $G$  defined over  $K$ , and a Zariski-dense subgroup  $\Gamma$  of  $G(K)$ , we prove that  $\Gamma$  contains a regular  $\mathbb{R}$ -regular element  $g$  such that the  $K$ -torus  $T := Z_G(g)^\circ$  is anisotropic over  $L$  and the cyclic subgroup generated by  $g$  is Zariski-dense in  $T$ . Existence of such elements allows us to settle questions of Margulis-Soifer, Hitchman-Spatzier and Benoist. Using these elements, we have also proved some results on the lengths of periodic geodesics in locally symmetric spaces. (Received January 13, 2005)